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CHAPTER 1

The CUBLAS Library

CUBLAS is an implementation of BLAS (Basic Linear Algebra Subprograms) on top of the NVIDIA® CUDA™ (compute unified device architecture) driver. It allows access to the computational resources of NVIDIA GPUs. The library is self-contained at the API level, that is, no direct interaction with the CUDA driver is necessary. CUBLAS attaches to a single GPU and does not auto-parallelize across multiple GPUs.

The basic model by which applications use the CUBLAS library is to create matrix and vector objects in GPU memory space, fill them with data, call a sequence of CUBLAS functions, and, finally, upload the results from GPU memory space back to the host. To accomplish this, CUBLAS provides helper functions for creating and destroying objects in GPU space, and for writing data to and retrieving data from these objects.

For maximum compatibility with existing Fortran environments, CUBLAS uses column-major storage and 1-based indexing. Since C and C++ use row-major storage, applications cannot use the native array semantics for two-dimensional arrays. Instead, macros or inline functions should be defined to implement matrices on top of one-dimensional arrays. For Fortran code ported to C in mechanical fashion, one may choose to retain 1-based indexing to avoid the need to
transform loops. In this case, the array index of a matrix element in row \( i \) and column \( j \) can be computed via the following macro:

\[
\text{IDX2F}(i, j, ld) = (((j)-1)*(ld))+((i)-1))
\]

Here, \( ld \) refers to the leading dimension of the matrix as allocated, which in the case of column-major storage is the number of rows. For natively written C and C++ code, one would most likely chose 0-based indexing, in which case the indexing macro becomes

\[
\text{IDX2C}(i, j, ld) = ((j)*(ld))+(i))
\]

Please refer to the code examples at the end of this section, which show a tiny application implemented in Fortran on the host (Example 1. “Fortran 77 Application Executing on the Host”) and show versions of the application written in C using CUBLAS for the indexing styles described above (Example 2. “Application Using C and CUBLAS: 1-based Indexing” and Example 3. “Application Using C and CUBLAS: 0-based Indexing”).

Because the CUBLAS core functions (as opposed to the helper functions) do not return error status directly (for reasons of compatibility with existing BLAS libraries), CUBLAS provides a separate function to aid in debugging that retrieves the last recorded error.

Currently, only a subset of the CUBLAS core functions is implemented.

The interface to the CUBLAS library is the header file \texttt{cublas.h}. Applications using CUBLAS need to link against the DSO \texttt{cublas.so} (Linux), the DLL \texttt{cublas.dll} (Windows), or the dynamic library \texttt{cublas.dylib} (Mac OS X) when building for the device, and against the DSO \texttt{cublasemu.so} (Linux), the DLL \texttt{cublasemu.dll} (Windows), or the dynamic library \texttt{cublasemu.dylib} (Mac OS X) when building for device emulation.

Following these three examples, the remainder of this chapter discusses “CUBLAS Types” on page 8 and “CUBLAS Helper Functions” on page 9.
Example 1. Fortran 77 Application Executing on the Host

```fortran
subroutine modify (m, ldm, n, p, q, alpha, beta)
imPLICIT none
integer ldm, n, p, q
real*4 m(ldm,*), alpha, beta
external sscal
Call sscal (n-p+1, alpha, m(p,q), ldm)
call sscal (ldm-p+1, beta, m(p,q), 1)
return
end

program matrixmod
implicit none
integer M, N
parameter (M=6, N=5)
real*4 a(M,N)
integer i, j
do j = 1, N
do i = 1, M
    a(i,j) = (i-1) * M + j
endo
dendo
call modify (a, M, N, 2, 3, 16.0, 12.0)
do j = 1, N
do i = 1, M
    write(*,",(F7.0$)") a(i,j)
dendo
enddo
write (*,*) ""
enddo
stop
end
```
Example 2. Application Using C and CUBLAS: 1-based Indexing

```c
#include <stdio.h>
#include <stdlib.h>
#include <math.h>
#include "cublas.h"

#define IDX2F(i,j,ld) (((j)-1)*(ld))+((i)-1))

tvoid modify (float *m, int ldm, int n, int p, int q, float alpha,
               float beta)
{
    cublasSscal (n-p+1, alpha, &m[IDX2F(p,q,ldm)], ldm);
    cublasSscal (ldm-p+1, beta, &m[IDX2F(p,q,ldm)], 1);
}

#define M 6
#define N 5
int main (void)
{
    int i, j;
    cublasStatus stat;
    float* devPtrA;
    float* a = 0;
    a = (float *)malloc (M * N * sizeof (*a));
    if (!a) {
        printf ("host memory allocation failed");
        return EXIT_FAILURE;
    }
    for (j = 1; j <= N; j++) {
        for (i = 1; i <= M; i++) {
            a[IDX2F(i,j,M)] = (i-1) * M + j;
        }
    }
    cublasInit();
    stat = cublasAlloc (M*N, sizeof(*a), (void**)&devPtrA);
```
CHAPTER 1

Example 2. Application Using C and CUBLAS: 1-based Indexing (continued)

```c
if (stat != CUBLAS_STATUS_SUCCESS) {
    printf("device memory allocation failed");
    cublasShutdown();
    return EXIT_FAILURE;
}
stat = cublasSetMatrix (M, N, sizeof(*a), a, M, devPtrA, M);
if (stat != CUBLAS_STATUS_SUCCESS) {
    printf("data download failed");
    cublasFree (devPtrA);
    cublasShutdown();
    return EXIT_FAILURE;
}
modify (devPtrA, M, N, 2, 3, 16.0f, 12.0f);
stat = cublasGetMatrix (M, N, sizeof(*a), devPtrA, M, a, M);
if (stat != CUBLAS_STATUS_SUCCESS) {
    printf("data upload failed");
    cublasFree (devPtrA);
    cublasShutdown();
    return EXIT_FAILURE;
}
cublasFree (devPtrA);
cublasShutdown();
for (j = 1; j <= N; j++) {
    for (i = 1; i <= M; i++) {
        printf("%7.0f", a[IDX2F(i,j,M)]);
    }
    printf("\n");
}
return EXIT_SUCCESS;
```
Example 3. Application Using C and CUBLAS: 0-based Indexing

```c
#include <stdio.h>
#include <stdlib.h>
#include <math.h>
#include "cublas.h"

#define IDX2C(i, j, ld) (((j)*(ld))+(i))

void modify (float *m, int ldm, int n, int p, int q, float alpha,
             float beta)
{    
cublasSscal (n-p, alpha, &m[IDX2C(p,q,ldm)], ldm);
cublasSscal (ldm-p, beta, &m[IDX2C(p,q,ldm)], 1);
}

#define M 6
#define N 5
int main (void)
{    
    int i, j;
cublasStatus stat;
float* devPtrA;
float* a = 0;
a = (float *)malloc (M * N * sizeof (*a));
if (!a) {
    printf ("host memory allocation failed");
    return EXIT_FAILURE;
}
for (j = 0; j < N; j++) {
    for (i = 0; i < M; i++) {
        a[IDX2C(i,j,M)] = i * M + j + 1;
    }
}
cublasInit();
stat = cublasAlloc (M*N, sizeof(*a), (void**) &devPtrA);
if (stat != CUBLAS_STATUS_SUCCESS) {
```
Example 3. Application Using C and CUBLAS: 0-based Indexing (continued)

```c
printf ("device memory allocation failed");
cublasShutdown();
return EXIT_FAILURE;
}
stat = cublasSetMatrix (M, N, sizeof(*a), a, M, devPtrA, M);
if (stat != CUBLAS_STATUS_SUCCESS) {
    printf ("data download failed");
cublasFree (devPtrA);
cublasShutdown();
    return EXIT_FAILURE;
}
modify (devPtrA, M, N, 1, 2, 16.0f, 12.0f);
stat = cublasGetMatrix (M, N, sizeof(*a), devPtrA, M, a, M);
if (stat != CUBLAS_STATUS_SUCCESS) {
    printf ("data upload failed");
cublasFree (devPtrA);
cublasShutdown();
    return EXIT_FAILURE;
}
cublasFree (devPtrA);
cublasShutdown();
for (j = 0; j < N; j++) {
    for (i = 0; i < M; i++) {
        printf ("%7.0f", a[IDX2C(i,j,M)]);
    }
    printf ("\n");
}
return EXIT_SUCCESS;
```
CUBLAS Types

The only CUBLAS type is `cublasStatus`.

Type `cublasStatus`

The type `cublasStatus` is used for function status returns. CUBLAS helper functions return status directly, while the status of CUBLAS core functions can be retrieved via `cublasGetError()`. Currently, the following values are defined:

<table>
<thead>
<tr>
<th><code>cublasStatus</code> Values</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>CUBLAS_STATUS_SUCCESS</code></td>
<td>operation completed successfully</td>
</tr>
<tr>
<td><code>CUBLAS_STATUS_NOT_INITIALIZED</code></td>
<td>CUBLAS library not initialized</td>
</tr>
<tr>
<td><code>CUBLAS_STATUS_ALLOC_FAILED</code></td>
<td>resource allocation failed</td>
</tr>
<tr>
<td><code>CUBLAS_STATUS_INVALID_VALUE</code></td>
<td>unsupported numerical value was passed to function</td>
</tr>
<tr>
<td><code>CUBLAS_STATUS_ARCH_MISMATCH</code></td>
<td>function requires an architectural feature absent from the architecture of</td>
</tr>
<tr>
<td></td>
<td>the device</td>
</tr>
<tr>
<td><code>CUBLAS_STATUS_MAPPING_ERROR</code></td>
<td>access to GPU memory space failed</td>
</tr>
<tr>
<td><code>CUBLAS_STATUS_EXECUTION_FAILED</code></td>
<td>GPU program failed to execute</td>
</tr>
<tr>
<td><code>CUBLAS_STATUS_INTERNAL_ERROR</code></td>
<td>an internal CUBLAS operation failed</td>
</tr>
</tbody>
</table>
CUBLAS Helper Functions

The following are the CUBLAS helper functions:

- “Function cublasInit()” on page 9
- “Function cublasShutdown()” on page 10
- “Function cublasGetError()” on page 10
- “Function cublasAlloc()” on page 10
- “Function cublasFree()” on page 11
- “Function cublasSetVector()” on page 11
- “Function cublasGetVector()” on page 12
- “Function cublasSetMatrix()” on page 13
- “Function cublasGetMatrix()” on page 13

Function cublasInit()

cublasStatus

__cublasInit (void)

initializes the CUBLAS library and must be called before any other
CUBLAS API function is invoked. It allocates hardware resources
necessary for accessing the GPU. It attaches CUBLAS to whatever
GPU is currently bound to the host thread from which it was invoked.

Return Values

<table>
<thead>
<tr>
<th>CUBLAS_STATUS_ALLOC_FAILED</th>
<th>if resources could not be allocated</th>
</tr>
</thead>
<tbody>
<tr>
<td>CUBLAS_STATUS_SUCCESS</td>
<td>if CUBLAS library initialized successfully</td>
</tr>
</tbody>
</table>
Function cublasShutdown()

```c
void cublasShutdown()
```

Releases CPU-side resources used by the CUBLAS library. The release of GPU-side resources may be deferred until the application shuts down.

**Return Values**
- `CUBLAS_STATUS_NOT_INITIALIZED` if CUBLAS library was not initialized
- `CUBLAS_STATUS_SUCCESS` CUBLAS library shut down successfully

Function cublasGetError()

```c
void cublasGetError()
```

Returns the last error that occurred on invocation of any of the CUBLAS core functions. While the CUBLAS helper functions return status directly, the CUBLAS core functions do not, improving compatibility with those existing environments that do not expect BLAS functions to return status. Reading the error status via `cublasGetError()` resets the internal error state to `CUBLAS_STATUS_SUCCESS`.

Function cublasAlloc()

```c
void cublasAlloc(int n, int elemSize, void **devicePtr)
```

Creates an object in GPU memory space capable of holding an array of `n` elements, where each element requires `elemSize` bytes of storage. If the function call is successful, a pointer to the object in GPU memory space is placed in `devicePtr`. Note that this is a device pointer that cannot be dereferenced in host code. Function `cublasAlloc()` is a wrapper around `cudaMalloc()`. Device pointers returned by
cublasAlloc() can therefore be passed to any CUDA device kernels, not just CUBLAS functions.

Return Values

<table>
<thead>
<tr>
<th>Status</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CUBLAS_STATUS_NOT_INITIALIZED</td>
<td>if CUBLAS library was not initialized</td>
</tr>
<tr>
<td>CUBLAS_STATUS_INVALID_VALUE</td>
<td>if ( n \leq 0 ) or ( \text{elemSize} \leq 0 )</td>
</tr>
<tr>
<td>CUBLAS_STATUS_ALLOC_FAILED</td>
<td>if the object could not be allocated due to lack of resources.</td>
</tr>
<tr>
<td>CUBLAS_STATUS_SUCCESS</td>
<td>if storage was successfully allocated</td>
</tr>
</tbody>
</table>

Function cublasFree()

cublasStatus
cublasFree (const void *devicePtr)

destroys the object in GPU memory space referenced by devicePtr.

Return Values

<table>
<thead>
<tr>
<th>Status</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CUBLAS_STATUS_NOT_INITIALIZED</td>
<td>if CUBLAS library was not initialized</td>
</tr>
<tr>
<td>CUBLAS_STATUS_INTERNAL_ERROR</td>
<td>if the object could not be deallocated</td>
</tr>
<tr>
<td>CUBLAS_STATUS_SUCCESS</td>
<td>if object was deallocated successfully</td>
</tr>
</tbody>
</table>

Function cublasSetVector()

cublasStatus
cublasSetVector (int \( n \), int \( \text{elemSize} \), const void *\( x \),
int \( \text{incx} \), void *\( y \), int \( \text{incy} \))

copies \( n \) elements from a vector \( x \) in CPU memory space to a vector \( y \)
in GPU memory space. Elements in both vectors are assumed to have a
size of \( \text{elemSize} \) bytes. Storage spacing between consecutive elements
is \( \text{incx} \) for the source vector \( x \) and \( \text{incy} \) for the destination vector \( y \).
In general, \( y \) points to an object, or part of an object, allocated via
\text{cublasAlloc()}. Column-major format for two-dimensional matrices
is assumed throughout CUBLAS. If the vector is part of a matrix, a
vector increment equal to 1 accesses a (partial) column of the matrix.
Similarly, using an increment equal to the leading dimension of the matrix accesses a (partial) row.

Return Values

<table>
<thead>
<tr>
<th>Status</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CUBLAS_STATUS_NOT_INITIALIZED</td>
<td>if CUBLAS library was not initialized</td>
</tr>
<tr>
<td>CUBLAS_STATUS_INVALID_VALUE</td>
<td>if incx, incy, or elemSize &lt;= 0</td>
</tr>
<tr>
<td>CUBLAS_STATUS_MAPPING_ERROR</td>
<td>if error accessing GPU memory</td>
</tr>
<tr>
<td>CUBLAS_STATUS_SUCCESS</td>
<td>if operation completed successfully</td>
</tr>
</tbody>
</table>

Function `cublasGetVector()`

```c
void* (*cublasGetVector)(int n, int elemSize, const void *x, int incx, void *y, int incy)
```

copies \( n \) elements from a vector \( x \) in GPU memory space to a vector \( y \) in CPU memory space. Elements in both vectors are assumed to have a size of \( \text{elemSize} \) bytes. Storage spacing between consecutive elements is \( \text{incx} \) for the source vector \( x \) and \( \text{incy} \) for the destination vector \( y \). In general, \( x \) points to an object, or part of an object, allocated via `cublasAlloc()`. Column-major format for two-dimensional matrices is assumed throughout CUBLAS. If the vector is part of a matrix, a vector increment equal to \( 1 \) accesses a (partial) column of the matrix. Similarly, using an increment equal to the leading dimension of the matrix accesses a (partial) row.

Return Values

<table>
<thead>
<tr>
<th>Status</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CUBLAS_STATUS_NOT_INITIALIZED</td>
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</tr>
<tr>
<td>CUBLAS_STATUS_SUCCESS</td>
<td>if operation completed successfully</td>
</tr>
</tbody>
</table>
CHAPTER 1 The CUBLAS Library

Function cublasSetMatrix()

```c

cublasStatus

cublasSetMatrix (int rows, int cols, int elemSize,
                   const void *A, int lda, void *B,
                   int ldb)
```

copies a tile of rows×cols elements from a matrix A in CPU memory space to a matrix B in GPU memory space. Each element requires storage of elemSize bytes. Both matrices are assumed to be stored in column-major format, with the leading dimension (that is, the number of rows) of source matrix A provided in lda, and the leading dimension of destination matrix B provided in ldb. B is a device pointer that points to an object, or part of an object, that was allocated in GPU memory space via cublasAlloc().

Return Values

- **CUBLAS_STATUS_NOT_INITIALIZED** if CUBLAS library was not initialized
- **CUBLAS_STATUS_INVALID_VALUE** if rows or cols < 0; or elemSize, lda, or ldb <= 0
- **CUBLAS_STATUS_MAPPING_ERROR** if error accessing GPU memory
- **CUBLAS_STATUS_SUCCESS** if operation completed successfully

Function cublasGetMatrix()

```c

cublasStatus

cublasGetMatrix (int rows, int cols, int elemSize,
                   const void *A, int lda, void *B,
                   int ldb)
```

copies a tile of rows×cols elements from a matrix A in GPU memory space to a matrix B in CPU memory space. Each element requires storage of elemSize bytes. Both matrices are assumed to be stored in column-major format, with the leading dimension (that is, the number of rows) of source matrix A provided in lda, and the leading dimension of destination matrix B provided in ldb. A is a device
pointer that points to an object, or part of an object, that was allocated in GPU memory space via cUBLASAlloc().

Return Values

<table>
<thead>
<tr>
<th>Status</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CUBLAS_STATUS_NOT_INITIALIZED</td>
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</tbody>
</table>
Chapter 2

BLAS1 Functions

Level 1 Basic Linear Algebra Subprograms (BLAS1) are functions that perform scalar, vector, and vector-vector operations. The CUBLAS BLAS1 implementation is described in these sections:

- “Single-Precision BLAS1 Functions” on page 16
- “Single-Precision Complex BLAS1 Functions” on page 28
- “Double-Precision BLAS1 Functions” on page 41
- “Double-Precision Complex BLAS1 functions” on page 53 (Not yet implemented)
### Single-Precision BLAS1 Functions

The single-precision BLAS1 functions are as follows:

- “Function cublasIsamax()” on page 16
- “Function cublasIsamin()” on page 17
- “Function cublasSasum()” on page 18
- “Function cublasSaxpy()” on page 18
- “Function cublasScopy()” on page 19
- “Function cublasSdot()” on page 20
- “Function cublasSnrm2()” on page 21
- “Function cublasSrot()” on page 22
- “Function cublasSrotg()” on page 23
- “Function cublasSrotm()” on page 24
- “Function cublasSscal()” on page 26
- “Function cublasSswap()” on page 27

#### Function cublasIsamax()

```c
int cublasIsamax (int n, const float *x, int incx)
```

finds the smallest index of the maximum magnitude element of single-precision vector `x`; that is, the result is the first `i`, `i = 0` to `n-1`, that maximizes `abs(x[1+i*incx])`. The result reflects 1-based indexing for compatibility with Fortran.

**Input**
- `n` number of elements in input vector
- `x` single-precision vector with `n` elements
- `incx` storage spacing between elements of `x`

**Output**
returns the smallest index (returns zero if `n <= 0` or `incx <= 0`)

**Reference:** [http://www.netlib.org/blas/isamax.f](http://www.netlib.org/blas/isamax.f)
Error status for this function can be retrieved via `cublasGetError()`.

Error Status

<table>
<thead>
<tr>
<th>Error Status</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CUBLAS_STATUS_NOT_INITIALIZED</td>
<td>if CUBLAS library was not initialized</td>
</tr>
<tr>
<td>CUBLAS_STATUS_ALLOC_FAILED</td>
<td>if function could not allocate reduction buffer</td>
</tr>
<tr>
<td>CUBLAS_STATUS_EXECUTION_FAILED</td>
<td>if function failed to launch on GPU</td>
</tr>
</tbody>
</table>

Function cublasIsamin()

```c
int cublasIsamin (int n, const float *x, int incx)
```

finds the smallest index of the minimum magnitude element of single-precision vector `x`; that is, the result is the first `i, i = 0` to `n-1`, that minimizes `abs(x[1+i*incx])`. The result reflects 1-based indexing for compatibility with Fortran.

Input

- `n` number of elements in input vector
- `x` single-precision vector with `n` elements
- `incx` storage spacing between elements of `x`

Output

returns the smallest index (returns zero if `n <= 0` or `incx <= 0`)

Reference: [http://www.netlib.org/scilib/blass.f](http://www.netlib.org/scilib/blass.f)

Error status for this function can be retrieved via `cublasGetError()`.

Error Status

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<tbody>
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<td>if function failed to launch on GPU</td>
</tr>
</tbody>
</table>
Function cublasSasum()  

```c
float
cublasSasum (int n, const float *x, int incx)
```

Computes the sum of the absolute values of the elements of single-precision vector \( x \); that is, the result is the sum from \( i = 0 \) to \( n-1 \) of \( \text{abs}(x[1+i*\text{incx}]) \).

**Input**

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>n</td>
<td>number of elements in input vector</td>
</tr>
<tr>
<td>x</td>
<td>single-precision vector with ( n ) elements</td>
</tr>
<tr>
<td>incx</td>
<td>storage spacing between elements of ( x )</td>
</tr>
</tbody>
</table>

**Output**

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>returns the single-precision sum of absolute values</td>
</tr>
<tr>
<td></td>
<td>(returns zero if ( n \leq 0 ) or ( \text{incx} \leq 0 ), or if an error occurred)</td>
</tr>
</tbody>
</table>

Reference: [http://www.netlib.org/blas/sasum.f](http://www.netlib.org/blas/sasum.f)

Error status for this function can be retrieved via `cublasGetError()`.

**Error Status**

<table>
<thead>
<tr>
<th>Code</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CUBLAS_STATUS_NOT_INITIALIZED</td>
<td>if CUBLAS library was not initialized</td>
</tr>
<tr>
<td>CUBLAS_STATUS_ALLOC_FAILED</td>
<td>if function could not allocate reduction buffer</td>
</tr>
<tr>
<td>CUBLAS_STATUS_EXECUTION_FAILED</td>
<td>if function failed to launch on GPU</td>
</tr>
</tbody>
</table>

Function cublasSaxpy()  

```c
void
cublasSaxpy (int n, float alpha, const float *x, int incx, float *y, int incy)
```

Multiplies single-precision vector \( x \) by single-precision scalar \( \alpha \) and adds the result to single-precision vector \( y \); that is, it overwrites single-precision \( y \) with single-precision \( \alpha \cdot x + y \).

For \( i = 0 \) to \( n-1 \), it replaces

\[
y[ly+i*incy] \quad \text{with} \quad \alpha \cdot x[lx+i*incx] + y[ly+i*incy],
\]
where
\[
1x = 1 \text{ if incx} \geq 0, \quad \text{else} \\
1x = 1 + (1 - n) \cdot \text{incx};
\]

\( ly \) is defined in a similar way using incy.

Input
- \( n \) number of elements in input vectors
- \( \alpha \) single-precision scalar multiplier
- \( x \) single-precision vector with \( n \) elements
- \( \text{incx} \) storage spacing between elements of \( x \)
- \( y \) single-precision vector with \( n \) elements
- \( \text{incy} \) storage spacing between elements of \( y \)

Output
- \( y \) single-precision result (unchanged if \( n \leq 0 \))

Reference: [http://www.netlib.org/blas/saxpy.f](http://www.netlib.org/blas/saxpy.f)

Error status for this function can be retrieved via \text{cublasGetError}().

Error Status
- \text{CUBLAS_STATUS_NOT_INITIALIZED} if CUBLAS library was not initialized
- \text{CUBLAS_STATUS_EXECUTION_FAILED} if function failed to launch on GPU

Function \text{cublasScopy()}

```c
void 
cublasScopy (int n, const float *x, int incx, float *y, 
               int incy)
```

copies the single-precision vector \( x \) to the single-precision vector \( y \). For \( i = 0 \) to \( n-1 \), it copies
\[
x[1x+i*\text{incx}] \text{ to } y[ly+i*\text{incy}],
\]
where
\[
1x = 1 \text{ if incx} \geq 0, \quad \text{else} \\
1x = 1 + (1 - n) \cdot \text{incx};
\]
ly is defined in a similar way using incy.

Input

\[
\begin{align*}
n & \text{ number of elements in input vectors} \\
x & \text{ single-precision vector with } n \text{ elements} \\
\text{incx} & \text{ storage spacing between elements of } x \\
y & \text{ single-precision vector with } n \text{ elements} \\
\text{incy} & \text{ storage spacing between elements of } y
\end{align*}
\]

Output

\[
\begin{align*}
y & \text{ contains single-precision vector } x
\end{align*}
\]

Reference: [http://www.netlib.org/blas/scopy.f](http://www.netlib.org/blas/scopy.f)

Error status for this function can be retrieved via `cublasGetError()`.

Error Status

- `CUBLAS_STATUS_NOT_INITIALIZED` if CUBLAS library was not initialized
- `CUBLAS_STATUS_EXECUTION_FAILED` if function failed to launch on GPU

Function `cublasSdot()`

```c
float
cublasSdot (int n, const float *x, int incx, const float *y, int incy)
```

computes the dot product of two single-precision vectors. It returns the dot product of the single-precision vectors x and y if successful, and 0.0f otherwise. It computes the sum for i = 0 to n-1 of

\[
x[lx+i*\text{incx}] * y[ly+i*\text{incy}],
\]

where

\[
\begin{align*}
\text{lx} & = 1 \text{ if incx} \geq 0, \text{else} \\
\text{lx} & = 1 + (1-n) * \text{incx};
\end{align*}
\]

ly is defined in a similar way using incy.

Input

\[
\begin{align*}
n & \text{ number of elements in input vectors} \\
x & \text{ single-precision vector with } n \text{ elements}
\end{align*}
\]
CHAPTER 2

BLAS1 Functions

Function cublasSnrm2()

float
cublasSnrm2 (int n, const float *x, int incx)
computes the Euclidean norm of the single-precision n-vector x (with storage increment incx). This code uses a multiphase model of accumulation to avoid intermediate underflow and overflow.

Input

n number of elements in input vector
x single-precision vector with n elements
incx storage spacing between elements of x

Output

returns the Euclidian norm
(returns zero if n <= 0, incx <= 0, or if an error occurred)

Reference: http://www.netlib.org/blas/snrm2.f
Reference: http://www.netlib.org/slatec/lin/snrm2.f

Reference:
http://www.netlib.org/blas/sdot.f

Error status for this function can be retrieved via cublasGetError().

Error Status

CUBLAS_STATUS_NOT_INITIALIZED if CUBLAS library was not initialized
CUBLAS_STATUS_ALLOC_FAILED if function could not allocate reduction buffer
CUBLAS_STATUS_EXECUTION_FAILED if function failed to execute on GPU

Input (continued)

incx storage spacing between elements of x
y single-precision vector with n elements
incy storage spacing between elements of y

Output

returns single-precision dot product (returns zero if n <= 0)
Error status for this function can be retrieved via `cublasGetError()`.  

**Error Status**  
<table>
<thead>
<tr>
<th>Status</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CUBLAS_STATUS_NOT_INITIALIZED</td>
<td>if CUBLAS library was not initialized</td>
</tr>
<tr>
<td>CUBLAS_STATUS_ALLOC_FAILED</td>
<td>if function could not allocate reduction buffer</td>
</tr>
<tr>
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<td>if function failed to launch on GPU</td>
</tr>
</tbody>
</table>

**Function cublasSrot()**  
```c
void
cublasSrot (int n, float *x, int incx, float *y, int incy,
        float sc, float ss)
```

multiplies a $2 \times 2$ matrix
\[
\begin{pmatrix}
sc & ss \\
-ss & sc
\end{pmatrix}
\]
with the $2 \times n$ matrix
\[
\begin{pmatrix}
x^T \\
y^T
\end{pmatrix}.
\]

The elements of $x$ are in $x[lx+i \times incx], i = 0$ to $n-1$, where
\[
lx = 1 \text{ if } incx \geq 0, \text{ else } \\
lx = 1 + (1-n) \times incx;
\]
y is treated similarly using $ly$ and $incy$.  

**Input**  
- $n$: number of elements in input vectors  
- $x$: single-precision vector with $n$ elements  
- $incx$: storage spacing between elements of $x$  
- $y$: single-precision vector with $n$ elements  
- $incy$: storage spacing between elements of $y$  
- $sc$: element of rotation matrix  
- $ss$: element of rotation matrix  

**Output**  
- $x$: rotated vector $x$ (unchanged if $n \leq 0$)  
- $y$: rotated vector $y$ (unchanged if $n \leq 0$)  

Reference: [http://www.netlib.org/blas/srot.f](http://www.netlib.org/blas/srot.f)
Error status for this function can be retrieved via 
\textbf{cublasGetError()}.

\textbf{Error Status}

\begin{itemize}
\item \texttt{CUBLAS\_STATUS\_NOT\_INITIALIZED} if CUBLAS library was not initialized
\item \texttt{CUBLAS\_STATUS\_EXECUTION\_FAILED} if function failed to launch on GPU
\end{itemize}

\textbf{Function cublasSrotg()}

\begin{verbatim}
void
cublasSrotg (float *sa, float *sb, float *sc, float *ss)
\end{verbatim}

constructs the Givens transformation

\[
G = \begin{bmatrix}
sc & ss \\
-ss & sc
\end{bmatrix}, \quad sc^2 + ss^2 = 1
\]

which zeros the second entry of the 2-vector \[\begin{bmatrix} sa & sb \end{bmatrix}^T\].

The quantity \( r = \pm \sqrt{sa^2 + sb^2} \) overwrites \( sa \) in storage. The value of \( sb \) is overwritten by a value \( z \) which allows \( sc \) and \( ss \) to be recovered by the following algorithm:

\begin{itemize}
\item if \( z = 1 \) set \( sc = 0.0 \) and \( ss = 1.0 \).
\item if \( \text{abs}(z) < 1 \) set \( sc = \sqrt{1-z^2} \) and \( ss = z \).
\item if \( \text{abs}(z) > 1 \) set \( sc = 1/z \) and \( ss = \sqrt{1-sc^2} \).
\end{itemize}

The function \textbf{cublasSrot}(n, x, incx, y, incy, sc, ss) normally is called next to apply the transformation to a \( 2 \times n \) matrix.

\textbf{Input}

\begin{itemize}
\item \( sa \) single-precision scalar
\item \( sb \) single-precision scalar
\end{itemize}

\textbf{Output}

\begin{itemize}
\item \( sa \) single-precision \( r \)
\item \( sb \) single-precision \( z \)
\item \( sc \) single-precision result
\item \( ss \) single-precision result
\end{itemize}
This function does not set any error status.

Function cublasSrotm()

```c
void cublasSrotm (int n, float *x, int incx, float *y, int incy, const float *sparam)
```

applies the modified Givens transformation, $h$, to the $2 \times n$ matrix

\[
\begin{bmatrix}
  x^T \\
  y^T
\end{bmatrix}
\]

The elements of $x$ are in $x[lx + i \cdot incx], i = 0$ to $n-1$, where

\[
lx = 1 \text{ if } incx \geq 0, \text{ else } lx = 1 + (1 - n) \cdot incx;
\]

$y$ is treated similarly using $ly$ and $incy$.

With $sparam[0] = sflag$, $h$ has one of the following forms:

- $sflag = -1.0f$  
  $h = \begin{bmatrix} sh00 & sh01 \\ sh10 & sh11 \end{bmatrix}$
- $sflag = 1.0f$  
  $h = \begin{bmatrix} 1.0f & sh01 \\ sh10 & 1.0f \end{bmatrix}$
- $sflag = 0.0f$  
  $h = \begin{bmatrix} sh00 & 1.0f \\ -1.0f & sh11 \end{bmatrix}$
- $sflag = -2.0f$  
  $h = \begin{bmatrix} 1.0f & 0.0f \\ 0.0f & 1.0f \end{bmatrix}$

**Input**

- $n$ number of elements in input vectors.
- $x$ single-precision vector with $n$ elements.
- $incx$ storage spacing between elements of $x$.
- $y$ single-precision vector with $n$ elements.
- $incy$ storage spacing between elements of $y$.
Output

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>x</td>
<td>rotated vector x (unchanged if n &lt;= 0)</td>
</tr>
<tr>
<td>y</td>
<td>rotated vector y (unchanged if n &lt;= 0)</td>
</tr>
</tbody>
</table>

Reference: [http://www.netlib.org/blas/srotm.f](http://www.netlib.org/blas/srotm.f)

Error status for this function can be retrieved via `cublasGetError()`.

Error Status

<table>
<thead>
<tr>
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<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CUBLAS_STATUS_NOT_INITIALIZED</td>
<td>if CUBLAS library was not initialized</td>
</tr>
<tr>
<td>CUBLAS_STATUS_EXECUTION_FAILED</td>
<td>if function failed to launch on GPU</td>
</tr>
</tbody>
</table>

Function `cublasSrotmg()`

```c
void
cublasSrotmg (float *sd1, float *sd2, float *sx1,
             const float *sy1, float *sparam)
```

constructs the modified Givens transformation matrix $h$ which zeros the second component of the 2-vector $(\sqrt{sd1} \cdot sx1, \sqrt{sd2} \cdot sy1)^T$.

With `sparam[0] = sflag`, $h$ has one of the following forms:

$sflag = -1.0f$

$$h = \begin{bmatrix}
    s00 & s01 \\
    sh10 & sh11
\end{bmatrix}$$

$sflag = 0.0f$

$$h = \begin{bmatrix}
    1.0f & s01 \\
    sh10 & 1.0f
\end{bmatrix}$$

$sflag = 1.0f$

$$h = \begin{bmatrix}
    s00 & 1.0f \\
    -1.0f & sh11
\end{bmatrix}$$

$sflag = -2.0f$

$$h = \begin{bmatrix}
    1.0f & 0.0f \\
    0.0f & 1.0f
\end{bmatrix}$$

`sparam[1] through sparam[4] contain s00, sh10, s01, and sh11, respectively. Values of 1.0f, -1.0f, or 0.0f implied by the value of `sflag` are not stored in `sparam`.

Input

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>sd1</td>
<td>single-precision scalar.</td>
</tr>
<tr>
<td>sd2</td>
<td>single-precision scalar.</td>
</tr>
<tr>
<td>sx1</td>
<td>single-precision scalar.</td>
</tr>
<tr>
<td>sy1</td>
<td>single-precision scalar.</td>
</tr>
</tbody>
</table>
**Function cublasSscal()**

```c
void cublasSscal (int n, float alpha, float *x, int incx)
```

replaces single-precision vector `x` with single-precision `alpha * x`. For
i = 0 to n-1, it replaces
```
x[lx+i*incx] with alpha * x[lx+i*incx],
```
where
```
lx = 1 if incx >= 0, else
lx = 1+(1-n) * incx.
```

**Input**
- `n` number of elements in input vector
- `alpha` single-precision scalar multiplier
- `x` single-precision vector with `n` elements
- `incx` storage spacing between elements of `x`

**Output**
- `x` single-precision result (unchanged if `n <= 0` or `incx <= 0`)

Reference: [http://www.netlib.org/blas/sscal.f](http://www.netlib.org/blas/sscal.f)
Error status for this function can be retrieved via \texttt{cublasGetError()}.

\textbf{Error Status}

\begin{tabular}{|l|l|}
\hline
\texttt{CUBLAS\_STATUS\_NOT\_INITIALIZED} & if CUBLAS library was not initialized \\
\texttt{CUBLAS\_STATUS\_EXECUTION\_FAILED} & if function failed to launch on GPU \\
\hline
\end{tabular}

\textbf{Function \texttt{cublasSswap()}}

\begin{verbatim}
void 
cublasSswap (int n, float *x, int incx, float *y, 
    int incy)
\end{verbatim}

interchanges single-precision vector \( x \) with single-precision vector \( y \).
For \( i = 0 \) to \( n-1 \), it interchanges
\[ x[lx+i*incx] \text{ with } y[ly+i*incy], \]
where
\[ lx = 1 \text{ if } incx \geq 0, \text{else} \]
\[ lx = 1+(1-n)*incx; \]
\( ly \) is defined in a similar manner using \( incy \).

\textbf{Input}

\begin{itemize}
    \item \texttt{n} number of elements in input vectors
    \item \texttt{x} single-precision vector with \texttt{n} elements
    \item \texttt{incx} storage spacing between elements of \texttt{x}
    \item \texttt{y} single-precision vector with \texttt{n} elements
    \item \texttt{incy} storage spacing between elements of \texttt{y}
\end{itemize}

\textbf{Output}

\begin{itemize}
    \item \texttt{x} input vector \( y \) (unchanged if \( n \leq 0 \))
    \item \texttt{y} input vector \( x \) (unchanged if \( n \leq 0 \))
\end{itemize}

\textbf{Reference:} \url{http://www.netlib.org/blas/sswap.f}

Error status for this function can be retrieved via \texttt{cublasGetError()}.

\textbf{Error Status}

\begin{tabular}{|l|l|}
\hline
\texttt{CUBLAS\_STATUS\_NOT\_INITIALIZED} & if CUBLAS library was not initialized \\
\texttt{CUBLAS\_STATUS\_EXECUTION\_FAILED} & if function failed to launch on GPU \\
\hline
\end{tabular}
Single-Precision Complex BLAS1 Functions

The single-precision complex BLAS1 functions are as follows:

- “Function cublasCaxpy()” on page 28
- “Function cublasCcopy()” on page 29
- “Function cublasCdotc()” on page 30
- “Function cublasCdotu()” on page 31
- “Function cublasCrot()” on page 32
- “Function cublasCrotg()” on page 33
- “Function cublasCscal()” on page 34
- “Function cublasCsrot()” on page 35
- “Function cublasCsscal()” on page 36
- “Function cublasCswap()” on page 37
- “Function cublasIcamax()” on page 37
- “Function cublasIcamin()” on page 38
- “Function cublasScasum()” on page 39
- “Function cublasScnrm2()” on page 40

Function cublasCaxpy()

```c
void
cublasCaxpy (int n, cuComplex alpha, const cuComplex *x,
               int incx, cuComplex *y, int incy)
```

multiplies single-precision complex vector x by single-precision complex scalar alpha and adds the result to single-precision complex vector y; that is, it overwrites single-precision complex y with single-precision complex alpha * x + y.

For i = 0 to n-1, it replaces

```c
y[ly+i*incy] with alpha * x[lx+i*incx] + y[ly+i*incy],
```

where

```c
lx = 0 if incx >= 0, else
lx = 1+(1-n)*incx;
```
ly is defined in a similar way using incy.

Input

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>n</td>
<td>number of elements in input vectors</td>
</tr>
<tr>
<td>alpha</td>
<td>single-precision complex scalar multiplier</td>
</tr>
<tr>
<td>x</td>
<td>single-precision complex vector with n elements</td>
</tr>
<tr>
<td>incx</td>
<td>storage spacing between elements of x</td>
</tr>
<tr>
<td>y</td>
<td>single-precision complex vector with n elements</td>
</tr>
<tr>
<td>incy</td>
<td>storage spacing between elements of y</td>
</tr>
</tbody>
</table>

Output

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>y</td>
<td>single-precision complex result (unchanged if n &lt;= 0)</td>
</tr>
</tbody>
</table>

Reference: [http://www.netlib.org/blas/caxpy.f](http://www.netlib.org/blas/caxpy.f)

Error status for this function can be retrieved via `cublasGetError()`. Error Status

- **CUBLAS_STATUS_NOT_INITIALIZED** if CUBLAS library was not initialized
- **CUBLAS_STATUS_EXECUTION_FAILED** if function failed to launch on GPU

Function `cublasCcopy()`

```c
void
cublasCcopy (int n, const cuComplex *x, int incx,
             cuComplex *y, int incy)
```

copies the single-precision complex vector `x` to the single-precision complex vector `y`.

For `i = 0` to `n-1`, it copies

\[ x[lx + i * incx] \rightarrow y[ly + i * incy], \]

where

\[ lx = 1 \text{ if } \text{incx} \geq 0, \text{ else } lx = 1 + (1 - n) \times \text{incx}; \]
ly is defined in a similar way using incy.

**Input**

- **n**: number of elements in input vectors
- **x**: single-precision complex vector with n elements
- **incx**: storage spacing between elements of x
- **y**: single-precision complex vector with n elements
- **incy**: storage spacing between elements of y

**Output**

- **y**: contains single-precision complex vector x

**Reference:** [http://www.netlib.org/blas/ccopy.f](http://www.netlib.org/blas/ccopy.f)

Error status for this function can be retrieved via `cublasGetError()`.

**Error Status**

- `CUBLAS_STATUS_NOT_INITIALIZED` if CUBLAS library was not initialized
- `CUBLAS_STATUS_EXECUTION_FAILED` if function failed to launch on GPU

### Function cublasCdotc()

```c
typedef struct cuComplex {
    float real; // Real part of the complex number
    float imag; // Imaginary part of the complex number
} cuComplex;

cublasStatus_t cublasCdotc(  
    int n,  
    const cuComplex *x, int incx,  
    const cuComplex *y, int incy)  
```

computes the dot product of two single-precision complex vectors, the first of which is conjugated. It returns the dot product of the complex conjugate of single-precision complex vector x and the single-precision complex vector y if successful, and complex zero otherwise. For i = 0 to n-1, it sums the products

\[ \text{x}[\text{l}x+i \times \text{incx}] \times \text{y}[\text{l}y+i \times \text{incy}], \]

where

- \( l_x = 1 \) if incx >= 0, else
- \( l_x = 1+(1-n) \times \text{incx} \);
ly is defined in a similar way using incy.

**Input**

- **n**: number of elements in input vectors
- **x**: single-precision complex vector with \( n \) elements
- **incx**: storage spacing between elements of \( x \)
- **y**: single-precision complex vector with \( n \) elements
- **incy**: storage spacing between elements of \( y \)

**Output**

returns single-precision complex dot product (zero if \( n \leq 0 \))

**Reference:** [http://www.netlib.org/blas/cdotc.f](http://www.netlib.org/blas/cdotc.f)

**Error Status**

- `CUBLAS_STATUS_NOT_INITIALIZED`: if CUBLAS library was not initialized
- `CUBLAS_STATUS_ALLOC_FAILED`: if function could not allocate reduction buffer
- `CUBLAS_STATUS_EXECUTION_FAILED`: if function failed to launch on GPU

**Function cublasCdotu()**

```c

cuComplex
cublasCdotu (int n, const cuComplex *x, int incx,
const cuComplex *y, int incy)
```

computes the dot product of two single-precision complex vectors. It returns the dot product of the single-precision complex vectors \( x \) and \( y \) if successful, and complex zero otherwise. For \( i = 0 \) to \( n-1 \), it sums the products

\[
x[lx + i * incx] \times y[ly + i * incy],
\]

where

- \( lx = 1 \) if \( incx \geq 0 \), else
- \( lx = 1 + (1 - n) * incx; \)
ly is defined in a similar way using incy.

**Input**

- **n**: number of elements in input vectors
- **x**: single-precision complex vector with n elements
- **incx**: storage spacing between elements of x
- **y**: single-precision complex vector with n elements
- **incy**: storage spacing between elements of y

**Output**

returns single-precision complex dot product (returns zero if n <= 0)

**Reference:** [http://www.netlib.org/blas/cdotu.f](http://www.netlib.org/blas/cdotu.f)

**Error Status**

- **CUBLAS_STATUS_NOT_INITIALIZED**: if CUBLAS library was not initialized
- **CUBLAS_STATUS_ALLOC_FAILED**: if function could not allocate reduction buffer
- **CUBLAS_STATUS_EXECUTION_FAILED**: if function failed to launch on GPU

**Function cublasCrot()**

```c
void cublasCrot (int n, cuComplex *x, int incx, cuComplex *y,
                int incy, float sc, cuComplex cs)
```

multiplies a $2\times2$ matrix

\[
\begin{pmatrix}
sc & cs \\
-cs & sc
\end{pmatrix}
\]

with the $2\times n$ matrix

\[
\begin{pmatrix}
x^T \\
y^T
\end{pmatrix}
\]

The elements of x are in $x[lx + i \times incx], i = 0$ to $n-1$, where

- $lx = 1$ if incx >= 0, else
- $lx = 1 + (1-n) \times incx$;

y is treated similarly using ly and incy.

**Input**

- **n**: number of elements in input vectors
- **x**: single-precision complex vector with n elements
CHAPTER 2 BLAS1 Functions

Input (continued)

- **incx**: storage spacing between elements of x
- **y**: single-precision complex vector with n elements
- **incy**: storage spacing between elements of y
- **sc**: single-precision cosine component of rotation matrix
- **cs**: single-precision complex sine component of rotation matrix

Output

- **x**: rotated vector x (unchanged if n <= 0)
- **y**: rotated vector y (unchanged if n <= 0)


Error status for this function can be retrieved via `cublasGetError()`.

Error Status

- **CUBLAS_STATUS_NOT_INITIALIZED**: if CUBLAS library was not initialized
- **CUBLAS_STATUS_EXECUTION_FAILED**: if function failed to launch on GPU

**Function cublasCrotg()**

```c
void
cublasCrotg (cuComplex *ca, cuComplex cb, float *sc, float *cs)
```

constructs the complex Givens transformation

\[
G = \begin{bmatrix}
sc & cs \\
-cs & sc
\end{bmatrix}, \quad sc*sc + cs*cs = 1
\]

which zeros the second entry of the complex 2-vector \([ca\ cb]^T\).

The quantity \(\frac{ca}{|ca|^2 + |cb|^2}\) overwrites \(ca\) in storage. In this case,

\[
||ca, cb|| = \frac{scale*\sqrt{|ca|/scale|^2 + |cb|/scale|^2}, where scale = |ca| + |cb|.
\]
The function `cublasCrot(n, x, incx, y, incy, sc, cs)` normally is called next to apply the transformation to a $2 \times n$ matrix.

**Input**

- **ca** single-precision complex scalar
- **cb** single-precision complex scalar

**Output**

- **ca** single-precision complex $\frac{ca}{|ca|} \cdot cb$
- **sc** single-precision cosine component of rotation matrix
- **cs** single-precision complex sine component of rotation matrix

Reference: [http://www.netlib.org/blas/crotg.f](http://www.netlib.org/blas/crotg.f)

This function does not set any error status.

**Function cublasCscal()**

```c
void
cublasCscal (int n, cuComplex alpha, cuComplex *x, int incx)
```

replaces single-precision complex vector $x$ with single-precision complex $\alpha \cdot x$.

For $i = 0$ to $n-1$, it replaces

$x[lx+i*incx]$ with $\alpha \cdot x[lx+i*incx]$,

where

- $lx = 1$ if $incx \geq 0$, else
- $lx = 1 + (1-n) \cdot incx$.

**Input**

- **n** number of elements in input vector
- **alpha** single-precision complex scalar multiplier
- **x** single-precision complex vector with $n$ elements
- **incx** storage spacing between elements of $x$

**Output**

- **x** single-precision complex result (unchanged if $n \leq 0$ or $incx \leq 0$)
Function cublasCsrot()

```c
void
cublasCsrot (int n, cuComplex *x, int incx, cuComplex *y,
               int incy, float sc, float ss)
```

multiplies a $2 \times 2$ matrix \[
\begin{bmatrix}
  sc & ss \\
  -ss & sc
\end{bmatrix}
\] with the $2 \times n$ matrix \[
\begin{bmatrix}
  x^T \\
  y^T
\end{bmatrix}
\].

The elements of $x$ are in $x[lx + i \times incx], i = 0$ to $n-1$, where

- $lx = 1$ if $incx \geq 0$,
- $lx = 1 + (1 - n) \times incx$;

$y$ is treated similarly using $ly$ and $incy$.

Input

- $n$ number of elements in input vectors
- $x$ single-precision complex vector with $n$ elements
- $incx$ storage spacing between elements of $x$
- $y$ single-precision complex vector with $n$ elements
- $incy$ storage spacing between elements of $y$
- $sc$ single-precision cosine component of rotation matrix
- $ss$ single-precision sine component of rotation matrix

Output

- $x$ rotated vector $x$ (unchanged if $n \leq 0$)
- $y$ rotated vector $y$ (unchanged if $n \leq 0$)

Reference: http://www.netlib.org/blas/csrot.f
Error status for this function can be retrieved via `cublasGetError()`.

### Error Status

- **CUBLAS_STATUS_NOT_INITIALIZED** if CUBLAS library was not initialized
- **CUBLAS_STATUS_EXECUTION_FAILED** if function failed to launch on GPU

### Function cublasCsscal()

```c
void cublasCsscal (int n, float alpha, cuComplex *x, int incx)
```

replaces single-precision complex vector `x` with single-precision complex `alpha` * `x`. For `i = 0` to `n-1`, it replaces

\[ x[lx+i}*incx] \text{ with } alpha * x[lx+i}*incx], \]

where

\[ lx = 1 \text{ if incx } \geq 0, \text{ else } \]
\[ lx = 1 + (1-n) * incx. \]

**Input**

- `n` number of elements in input vector
- `alpha` single-precision scalar multiplier
- `x` single-precision complex vector with `n` elements
- `incx` storage spacing between elements of `x`

**Output**

- `x` single-precision complex result (unchanged if `n` <= 0 or `incx` <= 0)

Reference: [http://www.netlib.org/blas/csscal.f](http://www.netlib.org/blas/csscal.f)

Error status for this function can be retrieved via `cublasGetError()`.

### Error Status

- **CUBLAS_STATUS_NOT_INITIALIZED** if CUBLAS library was not initialized
- **CUBLAS_STATUS_EXECUTION_FAILED** if function failed to launch on GPU
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Function cublasCswap()

```c
void
cublasCswap (int n, const cuComplex *x, int incx,
             cuComplex *y, int incy)
```

interchanges the single-precision complex vector \( x \) with the single-precision complex vector \( y \). For \( i = 0 \) to \( n-1 \), it interchanges

\[
x[lx+i*incx] \text{ with } y[ly+i*incy],
\]

where

\[
lx = 1 \text{ if incx } \geq 0, \text{ else } \\
1x = 1+(1-n)*incx;
\]

\( ly \) is defined in a similar way using \( incy \).

**Input**

- \( n \): number of elements in input vectors
- \( x \): single-precision complex vector with \( n \) elements
- \( incx \): storage spacing between elements of \( x \)
- \( y \): single-precision complex vector with \( n \) elements
- \( incy \): storage spacing between elements of \( y \)

**Output**

- \( x \): contains single-precision complex vector \( y \)
- \( y \): contains single-precision complex vector \( x \)

Reference: [http://www.netlib.org/blas/cswap.f](http://www.netlib.org/blas/cswap.f)

Error status for this function can be retrieved via `cublasGetError()`.

**Error Status**

- `CUBLAS_STATUS_NOT_INITIALIZED` if CUBLAS library was not initialized
- `CUBLAS_STATUS_EXECUTION_FAILED` if function failed to launch on GPU

Function cublasIcamax()

```c
int
cublasIcamax (int n, const cuComplex *x, int incx)
```

finds the smallest index of the maximum magnitude element of single-precision complex vector \( x \); that is, the result is the first \( i, i = 0 \) to \( n-1, \)
that maximizes \( \text{abs}(x[1+i \cdot \text{incx}]) \). The result reflects 1-based indexing for compatibility with Fortran.

Input

- \( n \): number of elements in input vector
- \( x \): single-precision complex vector with \( n \) elements
- \( \text{incx} \): storage spacing between elements of \( x \)

Output

returns the smallest index (returns zero if \( n \leq 0 \) or \( \text{incx} \leq 0 \))

Reference: http://www.netlib.org/blas/icamax.f

Error status for this function can be retrieved via `cublasGetError()`. Error Status

- `CUBLAS_STATUS_NOT_INITIALIZED`: if CUBLAS library was not initialized
- `CUBLAS_STATUS_ALLOC_FAILED`: if function could not allocate reduction buffer
- `CUBLAS_STATUS_EXECUTION_FAILED`: if function failed to launch on GPU

Function `cublasIcamin()`

```c
int cublasIcamin (int n, const cuComplex *x, int incx)
```

finds the smallest index of the minimum magnitude element of single-precision complex vector \( x \); that is, the result is the first \( i, i = 0 \) to \( n-1 \), that minimizes \( \text{abs}(x[1+i \cdot \text{incx}]) \). The result reflects 1-based indexing for compatibility with Fortran.

Input

- \( n \): number of elements in input vector
- \( x \): single-precision complex vector with \( n \) elements
- \( \text{incx} \): storage spacing between elements of \( x \)

Output

returns the smallest index (returns zero if \( n \leq 0 \) or \( \text{incx} \leq 0 \))

Reference: Analogous to http://www.netlib.org/blas/icamax.f
CHAPTER 2

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Error status for this function can be retrieved via `cublasGetError()`.

Error Status

<table>
<thead>
<tr>
<th>Error Status</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CUBLAS_STATUS_NOT_INITIALIZED</td>
<td>if CUBLAS library was not initialized</td>
</tr>
<tr>
<td>CUBLAS_STATUS_ALLOC_FAILED</td>
<td>if function could not allocate reduction buffer</td>
</tr>
<tr>
<td>CUBLAS_STATUS_EXECUTION_FAILED</td>
<td>if function failed to launch on GPU</td>
</tr>
</tbody>
</table>

Function `cublasScasum()`

```c
float
cublasScasum (int n, const cuDouble *x, int incx)
```

takes the sum of the absolute values of a complex vector and returns a single-precision result. Note that this is not the L1 norm of the vector. The result is the sum from 0 to n-1 of

\[
\text{abs}(\text{real}(x[lx+i*incx])) + \text{abs}(\text{imag}(x[lx+i*incx])),
\]

where

\[
x[lx] = 1 \text{ if } \text{incx} \leq 0, \text{ else } \\
x[lx] = 1 + (1-n) \cdot \text{incx}.
\]

Input

- **n**: number of elements in input vector
- **x**: single-precision complex vector with `n` elements
- **incx**: storage spacing between elements of `x`

Output

returns the single-precision sum of absolute values of real and imaginary parts (returns zero if `n \leq 0`, `incx \leq 0`, or if an error occurred)

Reference: [http://www.netlib.org/blas/scasum.f](http://www.netlib.org/blas/scasum.f)

Error status for this function can be retrieved via `cublasGetError()`.

Error Status

<table>
<thead>
<tr>
<th>Error Status</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CUBLAS_STATUS_NOT_INITIALIZED</td>
<td>if CUBLAS library was not initialized</td>
</tr>
<tr>
<td>CUBLAS_STATUS_ALLOC_FAILED</td>
<td>if function could not allocate reduction buffer</td>
</tr>
<tr>
<td>CUBLAS_STATUS_EXECUTION_FAILED</td>
<td>if function failed to launch on GPU</td>
</tr>
</tbody>
</table>
Function cublasScnrm2()

float
cublasScnrm2 (int n, const cuComplex *x, int incx)
computes the Euclidean norm of single-precision complex \( n \)-vector \( x \).
This implementation uses simple scaling to avoid intermediate underflow and overflow.

Input

\( n \)  number of elements in input vector \\
x  single-precision complex vector with \( n \) elements \\
incx  storage spacing between elements of \( x \)

Output

returns the Euclidian norm 
(returns zero if \( n \leq 0 \), \( \text{incx} \leq 0 \), or if an error occurred)


Error status for this function can be retrieved via `cublasGetError()`.

Error Status

- **CUBLAS_STATUS_NOT_INITIALIZED** if CUBLAS library was not initialized
- **CUBLAS_STATUS_ALLOC_FAILED** if function could not allocate reduction buffer
- **CUBLAS_STATUS_EXECUTION_FAILED** if function failed to launch on GPU
Double-Precision BLAS1 Functions

Note: Double-precision functions are only supported on GPUs with double-precision hardware.

The double-precision BLAS1 functions are as follows:

- “Function cublasIdamax()” on page 41
- “Function cublasIdamin()” on page 42
- “Function cublasDasum()” on page 43
- “Function cublasDaxpy()” on page 44
- “Function cublasDcopy()” on page 45
- “Function cublasDdot()” on page 46
- “Function cublasDnrm2()” on page 47
- “Function cublasDrot()” on page 47
- “Function cublasDrotg()” on page 48
- “Function cublasDrotm()” on page 49
- “Function cublasDrotmg()” on page 51
- “Function cublasDscal()” on page 52
- “Function cublasDswap()” on page 52

Function cublasIdamax()

```c
int
cublasIdamax (int n, const double *x, int incx)
```

finds the smallest index of the maximum magnitude element of double-precision vector \( x \); that is, the result is the first \( i, i = 0 \) to \( n-1 \), that maximizes \( \text{abs}(x[1+i*incx]) \). The result reflects 1-based indexing for compatibility with Fortran.

Input

<table>
<thead>
<tr>
<th>Input</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>( n )</td>
<td>number of elements in input vector</td>
</tr>
<tr>
<td>( x )</td>
<td>double-precision vector with ( n ) elements</td>
</tr>
<tr>
<td>( incx )</td>
<td>storage spacing between elements of ( x )</td>
</tr>
</tbody>
</table>
Function cublasIdamin()

```c
int
int cublasIdamin (int n, const double *x, int incx)
```

finds the smallest index of the minimum magnitude element of double-precision vector x; that is, the result is the first i, i = 0 to n-1, that minimizes \( |x[1 + i \times \text{incx}]| \). The result reflects 1-based indexing for compatibility with Fortran.

Input

- **n** number of elements in input vector
- **x** double-precision vector with n elements
- **incx** storage spacing between elements of x

Output

returns the smallest index (returns zero if n <= 0 or incx <= 0)

Analogous to [http://www.netlib.org/blas/idamax.f](http://www.netlib.org/blas/idamax.f)

Error status for this function can be retrieved via `cublasGetError()`.

Error Status

- **CUBLAS_STATUS_NOT_INITIALIZED** if CUBLAS library was not initialized
- **CUBLAS_STATUS_ALLOC_FAILED** if function could not allocate reduction buffer
- **CUBLAS_STATUS_ARCH_MISMATCH** if function invoked on device that does not support double precision
- **CUBLAS_STATUS_EXECUTION_FAILED** if function failed to launch on GPU
CHAPTER 2

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Function cublasDasum()

double
cublasDasum (int n, const double *x, int incx)

computes the sum of the absolute values of the elements of double-precision vector x; that is, the result is the sum from \( i = 0 \) to \( n-1 \) of \( \text{abs}(x[1+i*\text{incx}]) \).

Input

\( n \)  number of elements in input vector
\( x \)  double-precision vector with \( n \) elements
\( \text{incx} \)  storage spacing between elements of \( x \)

Output

returns the double-precision sum of absolute values
(returns zero if \( n \leq 0 \) or \( \text{incx} \leq 0 \), or if an error occurred)

Reference: [http://www.netlib.org/blas/dasum.f](http://www.netlib.org/blas/dasum.f)

Error status for this function can be retrieved via `cublasGetError()`.

Error Status

<table>
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<tr>
<td>CUBLAS_STATUS_NOT_INITIALIZED</td>
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<tr>
<td>CUBLAS_STATUS_ALLOC_FAILED</td>
<td>if function could not allocate reduction buffer</td>
</tr>
<tr>
<td>CUBLAS_STATUS_ARCH_MISMATCH</td>
<td>if function invoked on device that does not support double precision</td>
</tr>
<tr>
<td>CUBLAS_STATUS_EXECUTION_FAILED</td>
<td>if function failed to launch on GPU</td>
</tr>
</tbody>
</table>
Function cublasDaxpy()

```c
void
cublasDaxpy (int n, double alpha, const double *x,
             int incx, double *y, int incy)
```

multiplies double-precision vector \( x \) by double-precision scalar \( \alpha \) and adds the result to double-precision vector \( y \); that is, it overwrites double-precision \( y \) with double-precision \( \alpha \times x + y \).

For \( i = 0 \) to \( n-1 \), it replaces

\[ y[y + i \times \text{incy}] \text{ with } \alpha \times [x[x + i \times \text{incx}]] + y[y + i \times \text{incy}], \]

where

\[ lx = 1 \text{ if incx } \geq 0, \text{ else } \]
\[ lx = 1 + (1-n) \times \text{incx}; \]

\( ly \) is defined in a similar way using incy.

**Input**

- \( n \) number of elements in input vectors
- \( \alpha \) double-precision scalar multiplier
- \( x \) double-precision vector with \( n \) elements
- \( \text{incx} \) storage spacing between elements of \( x \)
- \( y \) double-precision vector with \( n \) elements
- \( \text{incy} \) storage spacing between elements of \( y \)

**Output**

- \( y \) double-precision result (unchanged if \( n \leq 0 \))

**Reference:** [http://www.netlib.org/blas/daxpy.f](http://www.netlib.org/blas/daxpy.f)

Error status for this function can be retrieved via `cublasGetError()`.

**Error Status**

- `CUBLAS_STATUS_NOT_INITIALIZED` if CUBLAS library was not initialized
- `CUBLAS_STATUS_ARCH_MISMATCH` if function invoked on device that does not support double precision
- `CUBLAS_STATUS_EXECUTION_FAILED` if function failed to launch on GPU
Function cublasDcopy()

```c
void
cublasDcopy (int n, const double *x, int incx, double *y, int incy)
```

copies the double-precision vector `x` to the double-precision vector `y`. For `i = 0` to `n-1`, it copies

\[ x[1x + i \times incx] \to y[1y + i \times incy], \]

where

\[
lx = 1 \text{ if incx } \geq 0, \text{ else } 1 + (1 - n) \times incx;\]

\(ly\) is defined in a similar way using `incy`.

**Input**

- `n` number of elements in input vectors
- `x` double-precision vector with `n` elements
- `incx` storage spacing between elements of `x`
- `y` double-precision vector with `n` elements
- `incy` storage spacing between elements of `y`

**Output**

- `y` contains double-precision vector `x`

Reference: [http://www.netlib.org/blas/dcopy.f](http://www.netlib.org/blas/dcopy.f)

Error status for this function can be retrieved via `cublasGetError()`.

**Error Status**

- `CUBLAS_STATUS_NOT_INITIALIZED` if CUBLAS library was not initialized
- `CUBLAS_STATUS_ARCH_MISMATCH` if function invoked on device that does not support double precision
- `CUBLAS_STATUS_EXECUTION_FAILED` if function failed to launch on GPU
Function cublasDdot()

double

cublasDdot (int n, const double *x, int incx,
        const double *y, int incy)

computes the dot product of two double-precision vectors. It returns
the dot product of the double-precision vectors x and y if successful,
and 0.0 otherwise. It computes the sum for i = 0 to n-1 of

\[ x[lx+i*incx] \cdot y[ly+i*incy], \]

where

\[ lx = 1 \text{ if incx} \geq 0, \text{ else} \]
\[ lx = 1+(1-n)*incx; \]
\[ ly \] is defined in a similar way using incy.

Input

- \( n \) number of elements in input vectors
- \( x \) double-precision vector with \( n \) elements
- \( \text{incx} \) storage spacing between elements of \( x \)
- \( y \) double-precision vector with \( n \) elements
- \( \text{incy} \) storage spacing between elements of \( y \)

Output

- returns double-precision dot product (returns zero if \( n \leq 0 \))

Reference: [http://www.netlib.org/blas/ddot.f](http://www.netlib.org/blas/ddot.f)

Error status for this function can be retrieved via `cublasGetError()`.

Error Status

- `CUBLAS_STATUS_NOT_INITIALIZED` if CUBLAS library was not initialized
- `CUBLAS_STATUS_ALLOC_FAILED` if function could not allocate
  reduction buffer
- `CUBLAS_STATUS_ARCH_MISMATCH` if function invoked on device that
  does not support double precision
- `CUBLAS_STATUS_EXECUTION_FAILED` if function failed to launch on GPU
Function `cublasDnrm2()`

```c
double

cublasDnrm2 (int n, const double *x, int incx)
```

computes the Euclidean norm of the double-precision `n`-vector `x` (with storage increment `incx`). This code uses a multiphase model of accumulation to avoid intermediate underflow and overflow.

**Input**

- `n` number of elements in input vector
- `x` double-precision vector with `n` elements
- `incx` storage spacing between elements of `x`

**Output**

returns the Euclidian norm

(returns zero if `n <= 0`, `incx <= 0`, or if an error occurred)

Reference: [http://www.netlib.org/blas/dnrm2.f](http://www.netlib.org/blas/dnrm2.f)

Error status for this function can be retrieved via `cublasGetError()`.

**Error Status**

- `CUBLAS_STATUS_NOT_INITIALIZED` if CUBLAS library was not initialized
- `CUBLAS_STATUS_ALLOC_FAILED` if function could not allocate reduction buffer
- `CUBLAS_STATUS_ARCH_MISMATCH` if function invoked on device that does not support double precision
- `CUBLAS_STATUS_EXECUTION_FAILED` if function failed to launch on GPU

Function `cublasDrot()`

```c
void
cublasDrot (int n, double *x, int incx, double *y, int incy, double dc, double ds)
```

multiplies a 2×2 matrix

\[
\begin{bmatrix}
dc & ds \\
n-ds & dc
\end{bmatrix}
\]

with the 2×n matrix

\[
\begin{bmatrix}
x^T \\
y^T
\end{bmatrix}
\]
The elements of $x$ are in $x[lx + i \cdot \text{incx}], i = 0 \text{ to } n-1$, where

\[
lx = 1 \text{ if incx} \geq 0, \text{ else} \\lx = 1 + (1-n) \cdot \text{incx};
\]

$y$ is treated similarly using $ly$ and $incy$.

**Input**

- $n$: number of elements in input vectors
- $x$: double-precision vector with $n$ elements
- $\text{incx}$: storage spacing between elements of $x$
- $y$: double-precision vector with $n$ elements
- $\text{incy}$: storage spacing between elements of $y$
- $dc$: element of rotation matrix
- $ds$: element of rotation matrix

**Output**

- $x$: rotated vector $x$ (unchanged if $n \leq 0$)
- $y$: rotated vector $y$ (unchanged if $n \leq 0$)

**Reference:** [http://www.netlib.org/blas/drot.f](http://www.netlib.org/blas/drot.f)

Error status for this function can be retrieved via `cublasGetError()`.

**Error Status**

- `CUBLAS_STATUS_NOT_INITIALIZED` if CUBLAS library was not initialized
- `CUBLAS_STATUS_ARCH_MISMATCH` if function invoked on device that does not support double precision
- `CUBLAS_STATUS_EXECUTION_FAILED` if function failed to launch on GPU

**Function cublasDrotg()**

```c
void
cublasDrotg (double *da, double *db, double *dc, double *ds)
```

constructs the Givens transformation

\[
G = \begin{bmatrix}
dc & ds \\
-ds & dc
\end{bmatrix}, \quad dc^2 + ds^2 = 1
\]

which zeros the second entry of the 2-vector $[da \ db]^T$. 

The quantity \( r = \pm \sqrt{da^2 + db^2} \) overwrites \( da \) in storage. The value of \( db \) is overwritten by a value \( z \) which allows \( dc \) and \( ds \) to be recovered by the following algorithm:

\[
\begin{align*}
\text{if } z &= 1 & \text{set } dc &= 0.0 \text{ and } ds = 1.0. \\
\text{if } \text{abs}(z) &< 1 & \text{set } dc &= \sqrt{1-z^2} \text{ and } ds = z. \\
\text{if } \text{abs}(z) &> 1 & \text{set } dc &= 1/z \text{ and } ds &= \sqrt{1-dc^2}.
\end{align*}
\]

The function `cublasDrot(n, x, incx, y, incy, dc, ds)` normally is called next to apply the transformation to a \( 2 \times n \) matrix.

**Input**

- \( da \) double-precision scalar
- \( db \) double-precision scalar

**Output**

- \( da \) double-precision \( r \)
- \( db \) double-precision \( z \)
- \( dc \) double-precision result
- \( ds \) double-precision result

Reference: [http://www.netlib.org/blas/drotg.f](http://www.netlib.org/blas/drotg.f)

This function does not set any error status.

**Function `cublasDrotm()`**

```c
void

cublasDrotm (int n, double *x, int incx, double *y, int incy, const double *dparam)
```

applies the modified Givens transformation, \( h \), to the \( 2 \times n \) matrix

\[
\begin{bmatrix}
x[i] \\
y[i]
\end{bmatrix}
\]

The elements of \( x \) are in \( x[1x+i*\text{incx}], i = 0 \text{ to } n-1, \) where

\[
1x = 1 \text{ if } \text{incx} >= 0, \text{ else } \\
1x = 1+(1-n)*\text{incx};
\]

\( y \) is treated similarly using \( 1y \) and \( \text{incy} \).
With \texttt{dparam[0] = dflag}, \texttt{h} has one of the following forms:

\[
\begin{align*}
\text{dflag} &= -1.0 & \text{dflag} &= 0.0 \\
h &= \begin{bmatrix} dh00 & dh01 \\ dh10 & dh11 \end{bmatrix} & h &= \begin{bmatrix} 1.0 & dh01 \\ dh10 & 1.0 \end{bmatrix} \\
\text{dflag} &= 1.0 & \text{dflag} &= -2.0 \\
h &= \begin{bmatrix} dh00 & 1.0 \\ -1.0 & dh11 \end{bmatrix} & h &= \begin{bmatrix} 1.0 & 0.0 \\ 0.0 & 1.0 \end{bmatrix}
\end{align*}
\]

\textbf{Input}

- \texttt{n} number of elements in input vectors.
- \texttt{x} double-precision vector with \texttt{n} elements.
- \texttt{incx} storage spacing between elements of \texttt{x}.
- \texttt{y} double-precision vector with \texttt{n} elements.
- \texttt{incy} storage spacing between elements of \texttt{y}.
- \texttt{dparam} 5-element vector. \texttt{dparam[0]} is \texttt{dflag} described above. \texttt{dparam[1]} through \texttt{dparam[4]} contain the 2×2 rotation matrix \texttt{h}: \texttt{dparam[1]} contains \texttt{dh00}, \texttt{dparam[2]} contains \texttt{dh10}, \texttt{dparam[3]} contains \texttt{dh01}, and \texttt{dparam[4]} contains \texttt{dh11}.

\textbf{Output}

- \texttt{x} rotated vector \texttt{x} (unchanged if \texttt{n} \leq 0)
- \texttt{y} rotated vector \texttt{y} (unchanged if \texttt{n} \leq 0)

\textbf{Reference:} [http://www.netlib.org/blas/drotm.f](http://www.netlib.org/blas/drotm.f)

Error status for this function can be retrieved via \texttt{cublasGetError()}. 

\textbf{Error Status}

- \texttt{CUBLAS_STATUS_NOT_INITIALIZED} if CUBLAS library was not initialized
- \texttt{CUBLAS_STATUS_ARCH_MISMATCH} if function invoked on device that does not support double precision
- \texttt{CUBLAS_STATUS_EXECUTION_FAILED} if function failed to launch on GPU
Function cublasDrotmg()  

```c
void
cublasDrotmg (double *dd1, double *dd2, double *dx1, 
               const double *dy1, double *dparam)
```

constructs the modified Givens transformation matrix \( h \) which zeros the second component of the 2-vector \((\sqrt{dd1} \cdot dx1, \sqrt{dd2} \cdot dy1)^T\).

With \( dparam[0] = dflag \), \( h \) has one of the following forms:

\[
\begin{align*}
\text{dflag} &= -1.0 & h &= \begin{bmatrix} dh00 & dh01 \\
                        dh10 & dh11 \end{bmatrix} \\
\text{dflag} &= 0.0 & h &= \begin{bmatrix} 1.0 & dh01 \\
                        dh10 & 1.0 \end{bmatrix} \\
\text{dflag} &= 1.0 & h &= \begin{bmatrix} dh00 & 1.0 \\
                   -1.0 & dh11 \end{bmatrix} \\
\text{dflag} &= -2.0 & h &= \begin{bmatrix} 1.0 & 0.0 \\
                   0.0 & 1.0 \end{bmatrix}
\end{align*}
\]

\( dparam[1] \) through \( dparam[4] \) contain \( dh00, dh10, dh01, \) and \( dh11, \) respectively. Values of \( 1.0, -1.0, \) or \( 0.0 \) implied by the value of \( dflag \) are not stored in \( dparam. \)

Input

- \( ddd1 \) double-precision scalar
- \( ddd2 \) double-precision scalar
- \( dx1 \) double-precision scalar
- \( dy1 \) double-precision scalar

Output

- \( ddd1 \) changed to represent the effect of the transformation
- \( ddd2 \) changed to represent the effect of the transformation
- \( dx1 \) changed to represent the effect of the transformation
- \( dparam \) 5-element vector. \( dparam[0] \) is \( dflag \) described above. \( dparam[1] \) through \( dparam[4] \) contain the 2×2 rotation matrix \( h; dparam[1] \) contains \( dh00, dparam[2] \) contains \( dh10, dparam[3] \) contains \( dh01, \) and \( dparam[4] \) contains \( dh11. \)

Reference: [http://www.netlib.org/blas/drotmg.f](http://www.netlib.org/blas/drotmg.f)

This function does not set any error status.
Function cublasDscal()

```c
void
cublasDscal (int n, double alpha, double *x, int incx)
```

replaces double-precision vector \( x \) with double-precision \( \alpha \times x \).
For \( i = 0 \) to \( n-1 \), it replaces

\[
x[lx+i*incx] \text{ with } \alpha \times [lx+i*incx],
\]

where

\[
lx = 1 \text{ if } incx >= 0, \text{ else } 1x = 1+(1-n) \times incx.
\]

Input

- \( n \) number of elements in input vector
- \( \alpha \) double-precision scalar multiplier
- \( x \) double-precision vector with \( n \) elements
- \( incx \) storage spacing between elements of \( x \)

Output

- \( x \) double-precision result (unchanged if \( n \leq 0 \) or \( incx \leq 0 \))

Reference: [http://www.netlib.org/blas/dscal.f](http://www.netlib.org/blas/dscal.f)

Error status for this function can be retrieved via `cublasGetError()`.

Error Status

- `CUBLAS_STATUS_NOT_INITIALIZED` if CUBLAS library was not initialized
- `CUBLAS_STATUS_ARCH_MISMATCH` if function invoked on device that does not support double precision
- `CUBLAS_STATUS_EXECUTION_FAILED` if function failed to launch on GPU

Function cublasDswap()

```c
void
cublasDswap (int n, double *x, int incx, double *y, int incy)
```

interchanges double-precision vector \( x \) with double-precision vector \( y \).
For \( i = 0 \) to \( n-1 \), it interchanges

\[
x[lx+i*incx] \text{ with } y[ly+i*incy],
\]
where
\[ \text{l}_x = \begin{cases} 1 & \text{if incx} \geq 0, \\ 1 + (1 - n) \times \text{incx} & \text{else} \end{cases} \]
\[ \text{l}_y \text{ is defined in a similar manner using incy.} \]

**Input**

- \( n \): number of elements in input vectors
- \( x \): double-precision vector with \( n \) elements
- \( \text{incx} \): storage spacing between elements of \( x \)
- \( y \): double-precision vector with \( n \) elements
- \( \text{incy} \): storage spacing between elements of \( y \)

**Output**

- \( x \): input vector \( y \) (unchanged if \( n \leq 0 \))
- \( y \): input vector \( x \) (unchanged if \( n \leq 0 \))

Reference: [http://www.netlib.org/blas/dswap.f](http://www.netlib.org/blas/dswap.f)

Error status for this function can be retrieved via `cublasGetError()`.  

**Error Status**

- **CUBLAS_STATUS_NOT_INITIALIZED**: if CUBLAS library was not initialized
- **CUBLAS_STATUS_ARCH_MISMATCH**: if function invoked on device that does not support double precision
- **CUBLAS_STATUS_EXECUTION_FAILED**: if function failed to launch on GPU

---

**Double-Precision Complex BLAS1 functions**

These functions have not been implemented yet.
CHAPTER 3

BLAS2 Functions

The Level 2 Basic Linear Algebra Subprograms (BLAS2) are functions that perform matrix-vector operations. The CUBLAS implementations are described in the following sections:

- “Single-Precision BLAS2 Functions” on page 55
- “Single-Precision Complex BLAS2 Functions” on page 76
  (Not yet implemented)
- “Double-Precision BLAS2 Functions” on page 77
- “Double-Precision Complex BLAS2 functions” on page 82
  (Not yet implemented)
Single-Precision BLAS2 Functions

The single-precision BLAS2 functions are as follows:

- “Function cublasSgbmv()” on page 55
- “Function cublasSgemv()” on page 57
- “Function cublasSger()” on page 58
- “Function cublasSsbmv()” on page 59
- “Function cublasSspmv()” on page 61
- “Function cublasSspr()” on page 62
- “Function cublasSspr2()” on page 63
- “Function cublasSsymv()” on page 64
- “Function cublasSsytr()” on page 65
- “Function cublasSsytr2()” on page 66
- “Function cublasStbmv()” on page 68
- “Function cublasStbsv()” on page 69
- “Function cublasStpmv()” on page 71
- “Function cublasStpsv()” on page 72
- “Function cublasStrmv()” on page 73
- “Function cublasStrsv()” on page 75

Function cublasSgbmv()

```c
void
cublasSgbmv (char trans, int m, int n, int kl, int ku,
  float alpha, const float *A, int lda,
  const float *x, int incx, float beta,
  float *y, int incy);
```

performs one of the matrix-vector operations

\[ y = \alpha \cdot \text{op}(A) \cdot x + \beta \cdot y, \]

where \( \text{op}(A) = A \) or \( \text{op}(A) = A^T \),
alpha and beta are single-precision scalars, and x and y are single-precision vectors. A is an m×n band matrix consisting of single-precision elements with kl subdiagonals and ku superdiagonals.

Input

trans specifies op(A). If trans == 'N' or 'n', op(A) = A.
If trans == 'T', 't', 'C', or 'c', op(A) = A'.
m the number of rows of matrix A; m must be at least zero.
n the number of columns of matrix A; n must be at least zero.
kl the number of subdiagonals of matrix A; kl must be at least zero.
ku the number of superdiagonals of matrix A; ku must be at least zero.
alpha single-precision scalar multiplier applied to op(A).
A single-precision array of dimensions (lda, n). The leading
(kl + ku + 1)×n part of array A must contain the band matrix A,
supplied column by column, with the leading diagonal of the matrix in
row ku+1 of the array, the first superdiagonal starting at position 2 in
row ku, the first subdiagonal starting at position 1 in row ku+2, and so
on. Elements in the array A that do not correspond to elements in the
band matrix (such as the top left ku×ku triangle) are not referenced.
lda leading dimension of A; lda must be at least kl + ku + 1.
x single-precision array of length at least (1 + (n−1) * abs(incx))
when trans == 'N' or 'n', and at least (1 + (m−1) * abs(incx))
otherwise.
incx storage spacing between elements of x; incx must not be zero.
beta single-precision scalar multiplier applied to vector y. If beta is zero, y
is not read.
y single-precision array of length at least (1 + (m−1) * abs(incy))
when trans == 'N' or 'n' and at least (1 + (n−1) * abs(incy))
otherwise. If beta is zero, y is not read.
incy storage spacing between elements of y; incy must not be zero.

Output

y updated according to y = alpha * op(A) * x + beta * y.

Reference: http://www.netlib.org/blas/sgbmv.f
CHAPTER 3 BLAS2 Functions

Error status for this function can be retrieved via `cublasGetError()`. 

**Error Status**

<table>
<thead>
<tr>
<th>Status</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>CUBLAS_STATUS_NOT_INITIALIZED</code></td>
<td>if CUBLAS library was not initialized</td>
</tr>
<tr>
<td><code>CUBLAS_STATUS_INVALID_VALUE</code></td>
<td>if m &lt; 0, n &lt; 0, kl &lt; 0, ku &lt; 0, incx == 0, or incy == 0</td>
</tr>
<tr>
<td><code>CUBLAS_STATUS_EXECUTION_FAILED</code></td>
<td>if function failed to launch on GPU</td>
</tr>
</tbody>
</table>

Function `cublasSgemv()`

```c
void
cublasSgemv (char trans, int m, int n, float alpha,
const float *A, int lda, const float *x,
int incx, float beta, float *y, int incy)
```

performs one of the matrix-vector operations

\[
y = \alpha \cdot \text{op}(A) \cdot x + \beta \cdot y,
\]

where \( \text{op}(A) = A \) or \( \text{op}(A) = A^T \),

\( \alpha \) and \( \beta \) are single-precision scalars, and \( x \) and \( y \) are single-precision vectors. \( A \) is an \( m \times n \) matrix consisting of single-precision elements. Matrix \( A \) is stored in column-major format, and \( \text{lda} \) is the leading dimension of the two-dimensional array in which \( A \) is stored.

**Input**

- `trans` specifies \( \text{op}(A) \). If \( \text{trans} = 'N' \) or \( 'n' \), \( \text{op}(A) = A \).
  - If \( \text{trans} = 'T', 't', 'C', \) or \( 'c' \), \( \text{op}(A) = A^T \).
- `m` specifies the number of rows of matrix \( A \); \( m \) must be at least zero.
- `n` specifies the number of columns of matrix \( A \); \( n \) must be at least zero.
- `alpha` single-precision scalar multiplier applied to \( \text{op}(A) \).
- `A` single-precision array of dimensions \( (\text{lda}, n) \) if \( \text{trans} = 'N' \) or \( 'n' \), of dimensions \( (\text{lda}, m) \) otherwise; \( \text{lda} \) must be at least \( \max(1, m) \) if \( \text{trans} = 'N' \) or \( 'n' \) and at least \( \max(1, n) \) otherwise.
- `lda` leading dimension of two-dimensional array used to store matrix \( A \).
- `x` single-precision array of length at least \( (1 + (n-1) \cdot \text{abs}(\text{incx})) \) if \( \text{trans} = 'N' \) or \( 'n' \), else at least \( (1 + (m-1) \cdot \text{abs}(\text{incx})) \).
- `incx` specifies the storage spacing for elements of \( x \); \( \text{incx} \) must not be zero.
- `beta` single-precision scalar multiplier applied to vector \( y \). If \( \beta \) is zero, \( y \) is not read.
CUDA

CUBLAS Library

Input (continued)

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>( m )</td>
<td>single-precision array of length at least ( 1 + (m-1) \cdot \text{abs}(\text{incy}) ) if ( \text{trans} == 'N' ) or 'n', else at least ( 1 + (n-1) \cdot \text{abs}(\text{incy}) ).</td>
</tr>
<tr>
<td>incy</td>
<td>the storage spacing between elements of ( y ); incy must not be zero.</td>
</tr>
</tbody>
</table>

Output

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>( y )</td>
<td>updated according to ( y = \alpha \cdot \text{op}(A) \cdot x + \beta \cdot y ).</td>
</tr>
</tbody>
</table>

Reference: [http://www.netlib.org/blas/sgemv.f](http://www.netlib.org/blas/sgemv.f)

Error status for this function can be retrieved via `cublasGetError()`.

Error Status

<table>
<thead>
<tr>
<th>Error Code</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CUBLAS_STATUS_NOT_INITIALIZED</td>
<td>if CUBLAS library was not initialized</td>
</tr>
<tr>
<td>CUBLAS_STATUS_INVALID_VALUE</td>
<td>if ( m &lt; 0, n &lt; 0, \text{incx} == 0 ), or incy == 0</td>
</tr>
<tr>
<td>CUBLAS_STATUS_EXECUTION_FAILED</td>
<td>if function failed to launch on GPU</td>
</tr>
</tbody>
</table>

Function `cublasSger()`

```c
void

cublasSger (int m, int n, float alpha, const float *x,
        int incx, const float *y, int incy, float *A,
        int lda)
```

performs the symmetric rank 1 operation

\[
A = \alpha \cdot x \cdot y^T + A,
\]

where \( \alpha \) is a single-precision scalar, \( x \) is an \( m \)-element single-precision vector, \( y \) is an \( n \)-element single-precision vector, and \( A \) is an \( m \times n \) matrix consisting of single-precision elements. Matrix \( A \) is stored in column-major format, and \( lda \) is the leading dimension of the two-dimensional array used to store \( A \).

Input

<table>
<thead>
<tr>
<th>Variable</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>( m )</td>
<td>specifies the number of rows of the matrix ( A ); ( m ) must be at least zero.</td>
</tr>
<tr>
<td>( n )</td>
<td>specifies the number of columns of matrix ( A ); ( n ) must be at least zero.</td>
</tr>
<tr>
<td>( \alpha )</td>
<td>single-precision scalar multiplier applied to ( x \cdot y^T ).</td>
</tr>
<tr>
<td>( x )</td>
<td>single-precision array of length at least ( 1 + (m-1) \cdot \text{abs}(\text{incx}) ).</td>
</tr>
<tr>
<td>incx</td>
<td>the storage spacing between elements of ( x ); incx must not be zero.</td>
</tr>
</tbody>
</table>
CHAPTER 3  BLAS2 Functions

**Input (continued)**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>y</td>
<td>single-precision array of length at least ((1 + (n-1) \times \text{abs(incy)})).</td>
</tr>
<tr>
<td>incy</td>
<td>the storage spacing between elements of (y); (\text{incy}) must not be zero.</td>
</tr>
<tr>
<td>A</td>
<td>single-precision array of dimensions ((\text{lda}, n)).</td>
</tr>
<tr>
<td>lda</td>
<td>leading dimension of two-dimensional array used to store matrix (A).</td>
</tr>
</tbody>
</table>

**Output**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>updated according to (A = \alpha \times x \times y^2 + A).</td>
</tr>
</tbody>
</table>

Reference: [http://www.netlib.org/blas/sger.f](http://www.netlib.org/blas/sger.f)

Error status for this function can be retrieved via \(\text{cublasGetError()}\).

**Error Status**

- **CUBLAS_STATUS_NOT_INITIALIZED** if CUBLAS library was not initialized
- **CUBLAS_STATUS_INVALID_VALUE** if \(m < 0, n < 0, \text{incx} == 0\), or \(\text{incy} == 0\)
- **CUBLAS_STATUS_EXECUTION_FAILED** if function failed to launch on GPU

---

**Function cublasSsbmv()**

```c
void
cublasSsbmv (char uplo, int n, int k, float alpha,
             const float *A, int lda, const float *x,
             int incx, float beta, float *y, int incy)
```

performs the matrix-vector operation

\[
y = \alpha \times A \times x + \beta \times y,
\]

where \(\alpha\) and \(\beta\) are single-precision scalars, and \(x\) and \(y\) are \(n\)-element single-precision vectors. \(A\) is an \(n \times n\) symmetric band matrix consisting of single-precision elements, with \(k\) superdiagonals and the same number of subdiagonals.

**Input**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>uplo</td>
<td>specifies whether the upper or lower triangular part of the symmetric band matrix (A) is being supplied. If (\text{uplo} == 'U') or ('u'), the upper triangular part is being supplied. If (\text{uplo} == 'L') or ('l'), the lower triangular part is being supplied.</td>
</tr>
<tr>
<td>n</td>
<td>specifies the number of rows and the number of columns of the symmetric matrix (A); (n) must be at least zero.</td>
</tr>
</tbody>
</table>
CUDA

Input (continued)

- **k** specifies the number of superdiagonals of matrix A. Since the matrix is symmetric, this is also the number of subdiagonals; k must be at least zero.
- **alpha** single-precision scalar multiplier applied to A * x.
- **A** single-precision array of dimensions (lda, n). When uplo == 'U' or 'u', the leading (k+1) x n part of array A must contain the upper triangular band of the symmetric matrix, supplied column by column, with the leading diagonal of the matrix in row k+1 of the array, the first superdiagonal starting at position 2 in row k, and so on. The top left k x k triangle of the array A is not referenced. When uplo == 'L' or 'l', the leading (k+1) x n part of the array A must contain the lower triangular band part of the symmetric matrix, supplied column by column, with the leading diagonal of the matrix in row 1 of the array, the first subdiagonal starting at position 1 in row 2, and so on. The bottom right k x k triangle of the array A is not referenced.
- **lda** leading dimension of A; lda must be at least k+1.
- **x** single-precision array of length at least (1 + (n-1) * abs(incx)).
- **incx** storage spacing between elements of x; incx must not be zero.
- **beta** single-precision scalar multiplier applied to vector y. If beta is zero, y is not read.
- **y** single-precision array of length at least (1 + (n-1) * abs(incy)). If beta is zero, y is not read.
- **incy** storage spacing between elements of y; incy must not be zero.

Output

- **y** updated according to y = alpha * A * x + beta * y.

Reference: [http://www.netlib.org/blas/ssbmv.f](http://www.netlib.org/blas/ssbmv.f)

Error status for this function can be retrieved via `cublasGetError()`.

Error Status

- **CUBLAS_STATUS_NOT_INITIALIZED** if CUBLAS library was not initialized
- **CUBLAS_STATUS_INVALID_VALUE** if k < 0, n < 0, incx == 0, or incy == 0
- **CUBLAS_STATUS_EXECUTION_FAILED** if function failed to launch on GPU
Function cublasSspmv()

```c
void
cublasSspmv (char uplo, int n, float alpha,
              const float *AP, const float *x, int incx,
              float beta, float *y, int incy)
```

performs the matrix-vector operation

\[ y = \alpha A \times x + \beta y, \]

where \( \alpha \) and \( \beta \) are single-precision scalars, and \( x \) and \( y \) are \( n \)-element single-precision vectors. \( A \) is a symmetric \( n \times n \) matrix that consists of single-precision elements and is supplied in packed form.

**Input**

- **uplo** specifies whether the matrix data is stored in the upper or the lower triangular part of array \( AP \). If \( uplo == 'U' \) or \( 'u' \), the upper triangular part of \( A \) is supplied in \( AP \). If \( uplo == 'L' \) or \( 'l' \), the lower triangular part of \( A \) is supplied in \( AP \).
- **n** is the number of rows and columns of matrix \( A \); \( n \) must be at least zero.
- **alpha** is the single-precision scalar multiplier applied to \( A \times x \).
- **AP** is a single-precision array with at least \((n \times (n+1))/2\) elements. If \( uplo == 'U' \) or \( 'u' \), array \( AP \) contains the upper triangular part of the symmetric matrix \( A \), packed sequentially, column by column; that is, if \( i \leq j \), \( A[i,j] \) is stored in \( AP[i+(j \times (j+1))/2] \). If \( uplo == 'L' \) or \( 'l' \), the array \( AP \) contains the lower triangular part of the symmetric matrix \( A \), packed sequentially, column by column; that is, if \( i \geq j \), \( A[i,j] \) is stored in \( AP[i+(2 \times n-j+1) \times j]/2] \).
- **x** is a single-precision array of length at least \((1+(n-1) \times \text{abs}(incx))\).
- **incx** is the storage spacing between elements of \( x \); \( incx \) must not be zero.
- **beta** is the single-precision scalar multiplier applied to vector \( y \). If \( beta \) is zero, \( y \) is not read.
- **y** is a single-precision array of length at least \((1+(n-1) \times \text{abs}(incy))\). If \( beta \) is zero, \( y \) is not read.
- **incy** is the storage spacing between elements of \( y \); \( incy \) must not be zero.

**Output**

- **y** is updated according to \( y = \alpha A \times x + \beta y \).

Reference: [http://www.netlib.org/blas/sspmv.f](http://www.netlib.org/blas/sspmv.f)
CUDA

Error status for this function can be retrieved via `cublasGetError()`.

### Error Status

- **CUBLAS_STATUS_NOT_INITIALIZED** if CUBLAS library was not initialized
- **CUBLAS_STATUS_INVALID_VALUE** if \( n < 0, \text{incx} == 0, \) or \( \text{incy} == 0 \)
- **CUBLAS_STATUS_EXECUTION_FAILED** if function failed to launch on GPU

### Function `cublasSspr()`

```c
void
cublasSspr (char uplo, int n, float alpha,
const float *x, int incx, float *AP)
```

performs the symmetric rank 1 operation

\[
A = \alpha \cdot x \cdot x^T + A,
\]

where \( \alpha \) is a single-precision scalar, and \( x \) is an \( n \)-element single-precision vector. \( A \) is a symmetric \( n \times n \) matrix that consists of single-precision elements and is supplied in packed form.

### Input

- **uplo** specifies whether the matrix data is stored in the upper or the lower triangular part of array \( A \). If \( \text{uplo} == 'U' \) or \( 'u' \), the upper triangular part of \( A \) is supplied in \( A \). If \( \text{uplo} == 'L' \) or \( 'l' \), the lower triangular part of \( A \) is supplied in \( A \).
- **n** the number of rows and columns of matrix \( A \); \( n \) must be at least zero.
- **alpha** single-precision scalar multiplier applied to \( x \cdot x^T \).
- **x** single-precision array of length at least \( (1 + (n-1) \cdot \text{abs(incx)}) \).
- **incx** storage spacing between elements of \( x \); \( \text{incx} \) must not be zero.
- **AP** single-precision array with at least \( (n \cdot (n+1))/2 \) elements. If \( \text{uplo} == 'U' \) or \( 'u' \), array \( AP \) contains the upper triangular part of the symmetric matrix \( A \), packed sequentially, column by column; that is, if \( i <= j, A[i,j] \) is stored in \( AP[i + (j \cdot (j+1)/2)] \). If \( \text{uplo} == 'L' \) or \( 'l' \), the array \( AP \) contains the lower triangular part of the symmetric matrix \( A \), packed sequentially, column by column; that is, if \( i >= j, A[i,j] \) is stored in \( AP[i + ((2 \cdot n - j + 1) \cdot j)/2] \).

### Output

- **A** updated according to \( A = \alpha \cdot x \cdot x^T + A \).

### Reference:

[http://www.netlib.org/blas/sspr.f](http://www.netlib.org/blas/sspr.f)
CHAPTER 3 BLAS2 Functions

Error status for this function can be retrieved via `cublasGetError()`.  

### Error Status

<table>
<thead>
<tr>
<th>Code</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>CUBLAS_STATUS_NOT_INITIALIZED</code></td>
<td>if CUBLAS library was not initialized</td>
</tr>
<tr>
<td><code>CUBLAS_STATUS_INVALID_VALUE</code></td>
<td>if <code>n &lt; 0</code> or <code>incx == 0</code></td>
</tr>
<tr>
<td><code>CUBLAS_STATUS_EXECUTION_FAILED</code></td>
<td>if function failed to launch on GPU</td>
</tr>
</tbody>
</table>

### Function cublasSspr2()

```c
void
cublasSspr2 (char uplo, int n, float alpha,
             const float *x, int incx, const float *y,
             int incy, float *AP)
```

performs the symmetric rank 2 operation

$$
A = \alpha x y^T + \alpha y x^T + A,
$$

where `alpha` is a single-precision scalar, and `x` and `y` are `n`-element single-precision vectors. `A` is a symmetric `n x n` matrix that consists of single-precision elements and is supplied in packed form.

### Input

- **uplo**: specifies whether the matrix data is stored in the upper or the lower triangular part of array `A`. If `uplo == 'U'` or `'u'`, only the upper triangular part of `A` may be referenced and the lower triangular part of `A` is inferred. If `uplo == 'L'` or `'l'`, only the lower triangular part of `A` may be referenced and the upper triangular part of `A` is inferred.
- **n**: the number of rows and columns of matrix `A`; `n` must be at least zero.
- **alpha**: single-precision scalar multiplier applied to `x y^T + \alpha y x^T`.
- **x**: single-precision array of length at least `(1 + (n-1) \cdot \text{abs}(\text{incx}))`.
- **incx**: storage spacing between elements of `x`; `incx` must not be zero.
- **y**: single-precision array of length at least `(1 + (n-1) \cdot \text{abs}(\text{incy}))`.
- **incy**: storage spacing between elements of `y`; `incy` must not be zero.
- **AP**: single-precision array with at least `(n \cdot (n + 1))/2` elements. If `uplo == 'U'` or `'u'`, array `AP` contains the upper triangular part of the symmetric matrix `A`, packed sequentially, column by column; that is, if `i <= j`, `A[i,j]` is stored in `AP[i+(j*(j+1)/2)]`. If `uplo == 'L'` or `'l'`, the array `AP` contains the lower triangular part of the symmetric matrix `A`, packed sequentially, column by column; that is, if `i >= j`, `A[i,j]` is stored in `AP[i+((2 \cdot n - j + 1) \cdot j)/2]`. 


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Output

\[ \mathbf{A} \text{ updated according to } \mathbf{A} = \alpha \mathbf{x} \mathbf{x}^T + \alpha \mathbf{y} \mathbf{y}^T + \mathbf{A}. \]

Reference: [http://www.netlib.org/blas/sspr2.f](http://www.netlib.org/blas/sspr2.f)

Error status for this function can be retrieved via `cublasGetError()`.

Error Status

- **CUBLAS_STATUS_NOT_INITIALIZED** if CUBLAS library was not initialized
- **CUBLAS_STATUS_INVALID_VALUE** if \( n < 0, \text{incx} == 0, \text{incy} == 0 \)
- **CUBLAS_STATUS_EXECUTION_FAILED** if function failed to launch on GPU

Function `cublasSsymv()`

```c
void

cublasSsymv (char uplo, int n, float alpha,
    const float *A, int lda, const float *x,
    int incx, float beta, float *y, int incy)
```

performs the matrix-vector operation

\[ y = \alpha \mathbf{A} \mathbf{x} + \beta \mathbf{y}, \]

where \( \alpha \) and \( \beta \) are single-precision scalars, and \( \mathbf{x} \) and \( \mathbf{y} \) are \( n \)-element single-precision vectors. \( \mathbf{A} \) is a symmetric \( n \times n \) matrix that consists of single-precision elements and is stored in either upper or lower storage mode.

Input

- **uplo** specifies whether the upper or lower triangular part of the array \( \mathbf{A} \) is referenced. If `uplo == 'U'` or `'u'`, the symmetric matrix \( \mathbf{A} \) is stored in upper storage mode; that is, only the upper triangular part of \( \mathbf{A} \) is referenced while the lower triangular part of \( \mathbf{A} \) is inferred. If `uplo == 'L'` or `'l'`, the symmetric matrix \( \mathbf{A} \) is stored in lower storage mode; that is, only the lower triangular part of \( \mathbf{A} \) is referenced while the upper triangular part of \( \mathbf{A} \) is inferred.
- **n** specifies the number of rows and the number of columns of the symmetric matrix \( \mathbf{A} \); \( n \) must be at least zero.
- **alpha** single-precision scalar multiplier applied to \( \mathbf{A} \mathbf{x} \).
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Input (continued)

| A     | single-precision array of dimensions (lda, n). If uplo == 'U' or 'u', the leading n\times n upper triangular part of the array A must contain the upper triangular part of the symmetric matrix and the strictly lower triangular part of A is not referenced. If uplo == 'L' or 'l', the leading n\times n lower triangular part of the array A must contain the lower triangular part of the symmetric matrix and the strictly upper triangular part of A is not referenced. |
| lda   | leading dimension of A; lda must be at least max(1, n). |
| x     | single-precision array of length at least (1 + (n - 1) * abs(incx)). |
| incx  | storage spacing between elements of x; incx must not be zero. |
| beta  | single-precision scalar multiplier applied to vector y. If beta is zero, y is not read. |
| y     | single-precision array of length at least (1 + (n - 1) * abs(incy)). If beta is zero, y is not read. |
| incy  | storage spacing between elements of y; incy must not be zero. |

Output

| y     | updated according to y = alpha * A * x + beta * y. |

Reference: [http://www.netlib.org/blas/ssymv.f](http://www.netlib.org/blas/ssymv.f)

Error status for this function can be retrieved via `cublasGetError()`. 

Error Status

- **CUBLAS_STATUS_NOT_INITIALIZED** if CUBLAS library was not initialized
- **CUBLAS_STATUS_INVALID_VALUE** if n < 0, incx == 0, or incy == 0
- **CUBLAS_STATUS_EXECUTION_FAILED** if function failed to launch on GPU

### Function cublasSsyr()

```c
void 
cublasSsyr (char uplo, int n, float alpha, 
            const float *x, int incx, float *A, int lda) 
```

performs the symmetric rank 1 operation

\[
A = \alpha x x^T + A, 
\]

where \( \alpha \) is a single-precision scalar, \( x \) is an \( n \)-element single-precision vector, and \( A \) is an \( n \times n \) symmetric matrix consisting of single-precision...
precision elements. A is stored in column-major format, and lda is the leading dimension of the two-dimensional array containing A.

Input

- **uplo** specifies whether the matrix data is stored in the upper or the lower triangular part of array A. If uplo == 'U' or 'u', only the upper triangular part of A is referenced. If uplo == 'L' or 'l', only the lower triangular part of A is referenced.
- **n** the number of rows and columns of matrix A; n must be at least zero.
- **alpha** single-precision scalar multiplier applied to x * x^T.
- **x** single-precision array of length at least (1 + (n-1) * abs(incx)).
- **incx** the storage spacing between elements of x; incx must not be zero.
- **A** single-precision array of dimensions (lda, n). If uplo == 'U' or 'u', A contains the upper triangular part of the symmetric matrix, and the strictly lower triangular part is not referenced. If uplo == 'L' or 'l', A contains the lower triangular part of the symmetric matrix, and the strictly upper triangular part is not referenced.
- **lda** leading dimension of the two-dimensional array containing A; lda must be at least max(1, n).

Output

A updated according to A = alpha * x * x^T + A.

Reference: [http://www.netlib.org/blas/ssyr.f](http://www.netlib.org/blas/ssyr.f)

Error status for this function can be retrieved via cublasGetError().

Error Status

- **CUBLAS_STATUS_NOT_INITIALIZED** if CUBLAS library was not initialized
- **CUBLAS_STATUS_INVALID_VALUE** if n < 0 or incx == 0
- **CUBLAS_STATUS_EXECUTION_FAILED** if function failed to launch on GPU

Function cublasSsyr2()

```c
void cublasSsyr2 (char uplo, int n, float alpha,
                const float *x, int incx, const float *y,
                int incy, float *A, int lda)
```

performs the symmetric rank 2 operation

A = alpha * x * y^T + alpha * y * x^T + A,
where \( \alpha \) is a single-precision scalar, \( x \) and \( y \) are \( n \)-element single-precision vectors, and \( A \) is an \( n \times n \) symmetric matrix consisting of single-precision elements.

### Input

- **\( \text{uplo} \)** specifies whether the matrix data is stored in the upper or the lower triangular part of array \( A \). If \( \text{uplo} = 'U' \) or 'u', only the upper triangular part of \( A \) is referenced and the lower triangular part of \( A \) is inferred. If \( \text{uplo} = 'L' \) or 'l', only the lower triangular part of \( A \) is referenced and the upper triangular part of \( A \) is inferred.
- **\( n \)** is the number of rows and columns of matrix \( A \); \( n \) must be at least zero.
- **\( \alpha \)** is a single-precision scalar multiplier applied to \( x \). \( x \) and \( y \) are \( n \)-element single-precision vectors.
- **\( \text{incx} \)** is the storage spacing between elements of \( x \); \( \text{incx} \) must not be zero.
- **\( y \)** is a single-precision array of length at least \( 1 + (n-1) \times \text{abs}(\text{incy}) \).
- **\( \text{incy} \)** is the storage spacing between elements of \( y \); \( \text{incy} \) must not be zero.
- **\( A \)** is a single-precision array of dimensions \( (\text{lda}, n) \). If \( \text{uplo} = 'U' \) or 'u', \( A \) contains the upper triangular part of the symmetric matrix, and the strictly lower triangular part is not referenced. If \( \text{uplo} = 'L' \) or 'l', \( A \) contains the lower triangular part of the symmetric matrix, and the strictly upper triangular part is not referenced.
- **\( \text{lda} \)** is the leading dimension of \( A \); \( \text{lda} \) must be at least \( \max(1, n) \).

### Output

\( A \) updated according to \( A = \alpha \times x \times y^T + \alpha \times y \times x^T + A \).

### Reference

[http://www.netlib.org/blas/ssyr2.f](http://www.netlib.org/blas/ssyr2.f)

Error status for this function can be retrieved via `cublasGetError()`.

### Error Status

- **\( \text{CUBLAS_STATUS_NOT_INITIALIZED} \)** if CUBLAS library was not initialized
- **\( \text{CUBLAS_STATUS_INVALID_VALUE} \)** if \( n < 0 \), \( \text{incx} = 0 \), or \( \text{incy} = 0 \)
- **\( \text{CUBLAS_STATUS_EXECUTION_FAILED} \)** if function failed to launch on GPU
Function cublasStbmv()

```c
void cublasStbmv (char uplo, char trans, char diag, int n,
                 int k, const float *A, int lda, float *x,
                 int incx)
```

performs one of the matrix-vector operations

\[ x = \text{op}(A) * x, \]

where \( \text{op}(A) = A \) or \( \text{op}(A) = A^T \),

\( x \) is an \( n \)-element single-precision vector, and \( A \) is an \( n \times n \), unit or non-unit, upper or lower, triangular band matrix consisting of single-precision elements.

**Input**

- **uplo** specifies whether the matrix \( A \) is an upper or lower triangular band matrix. If \( \text{uplo} == 'U' \) or \( 'u' \), \( A \) is an upper triangular band matrix. If \( \text{uplo} == 'L' \) or \( 'l' \), \( A \) is a lower triangular band matrix.
- **trans** specifies \( \text{op}(A) \). If \( \text{trans} == 'N' \) or \( 'n' \), \( \text{op}(A) = A \).
  If \( \text{trans} == 'T' \), \( 't' \), \( 'C' \), or \( 'c' \), \( \text{op}(A) = A^T \).
- **diag** specifies whether or not matrix \( A \) is unit triangular. If \( \text{diag} == 'U' \) or \( 'u' \), \( A \) is assumed to be unit triangular. If \( \text{diag} == 'N' \) or \( 'n' \), \( A \) is not assumed to be unit triangular.
- **n** specifies the number of rows and columns of the matrix \( A \); \( n \) must be at least zero. In the current implementation \( n \) must not exceed 4070.
- **k** specifies the number of superdiagonals or subdiagonals. If \( \text{uplo} == 'U' \) or \( 'u' \), \( k \) specifies the number of superdiagonals. If \( \text{uplo} == 'L' \) or \( 'l' \), \( k \) specifies the number of subdiagonals; \( k \) must at least be zero.
- **A** single-precision array of dimension \( (lda, n) \). If \( \text{uplo} == 'U' \) or \( 'u' \), the leading \( (k+1) \times n \) part of the array \( A \) must contain the upper triangular band matrix, supplied column by column, with the leading diagonal of the matrix in row \( k+1 \) of the array, the first superdiagonal starting at position 2 in row \( k \), and so on. The top left \( k \times k \) triangle of the array \( A \) is not referenced. If \( \text{uplo} == 'L' \) or \( 'l' \), the leading \( (k+1) \times n \) part of the array \( A \) must contain the lower triangular band matrix, supplied column by column, with the leading diagonal of the matrix in row 1 of the array, the first subdiagonal starting at position 1 in row 2, and so on. The bottom right \( k \times k \) triangle of the array is not referenced.
- **lda** is the leading dimension of \( A \); \( lda \) must be at least \( k+1 \).
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Reference: http://www.netlib.org/blas/stbmv.f

Error status for this function can be retrieved via cublasGetError().

Error Status

<table>
<thead>
<tr>
<th>Status</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CUBLAS_STATUS_NOT_INITIALIZED</td>
<td>if CUBLAS library was not initialized</td>
</tr>
<tr>
<td>CUBLAS_STATUS_INVALID_VALUE</td>
<td>if n &lt; 0, n &gt; 4070, k &lt; 0, or incx == 0</td>
</tr>
<tr>
<td>CUBLAS_STATUS_EXECUTION_FAILED</td>
<td>if function failed to launch on GPU</td>
</tr>
</tbody>
</table>

Function cublasStbsv()

```c
void
cublasStbsv (char uplo, char trans, char diag, int n,
             int k, const float *A, int lda, float X,
             int incx)
```

solves one of the systems of equations

\[
op(A) \times x = b,
\]

where \( \text{op}(A) = A \) or \( \text{op}(A) = A^T \),

\( b \) and \( x \) are n-element vectors, and \( A \) is an \( n \times n \), unit or non-unit, upper or lower, triangular band matrix with \( k+1 \) diagonals.

No test for singularity or near-singularity is included in this function. Such tests must be performed before calling this function.

Input

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>uplo</td>
<td>specifies whether the matrix is an upper or lower triangular band matrix: If uplo == 'U' or 'u', ( A ) is an upper triangular band matrix. If uplo == 'L' or 'l', ( A ) is a lower triangular band matrix.</td>
</tr>
<tr>
<td>trans</td>
<td>specifies ( \text{op}(A) ). If trans == 'N' or 'n', ( \text{op}(A) = A ). If trans == 'T', 't', 'C', or 'c', ( \text{op}(A) = A^T ).</td>
</tr>
</tbody>
</table>
Input (continued)

**diag** specifies whether A is unit triangular. If diag == 'U' or 'u', A is assumed to be unit triangular; that is, diagonal elements are not read and are assumed to be unity. If diag == 'N' or 'n', A is not assumed to be unit triangular.

**n** the number of rows and columns of matrix A; n must be at least zero.

**k** specifies the number of superdiagonals or subdiagonals.
If uplo == 'U' or 'u', k specifies the number of superdiagonals. If uplo == 'L' or 'l', k specifies the number of subdiagonals; k must be at least zero.

**A** single-precision array of dimension (lda, n). If uplo == 'U' or 'u', the leading (k+1)×n part of the array A must contain the upper triangular band matrix, supplied column by column, with the leading diagonal of the matrix in row k+1 of the array, the first superdiagonal starting at position 2 in row k, and so on. The top left k×k triangle of the array A is not referenced. If uplo == 'L' or 'l', the leading (k+1)×n part of the array A must contain the lower triangular band matrix, supplied column by column, with the leading diagonal of the matrix in row 1 of the array, the first sub-diagonal starting at position 1 in row 2, and so on. The bottom right k×k triangle of the array is not referenced.

**x** single-precision array of length at least (1+(n-1)×abs(incx)). On entry, x contains the n-element right-hand side vector b. On exit, it is overwritten with the solution vector x.

**incx** storage spacing between elements of x; incx must not be zero.

Output

**x** updated to contain the solution vector x that solves \( \text{op}(A) * x = b \).

Reference: [http://www.netlib.org/blas/stbsv.f](http://www.netlib.org/blas/stbsv.f)

Error status for this function can be retrieved via cublasGetError().

Error Status

- **CUBLAS_STATUS_NOT_INITIALIZED** if CUBLAS library was not initialized
- **CUBLAS_STATUS_INVALID_VALUE** if incx == 0, n < 0, or n > 4070
- **CUBLAS_STATUS_EXECUTION_FAILED** if function failed to launch on GPU
Function cublasStpmv()

```c
void
cublasStpmv (char uplo, char trans, char diag, int n,
        const float *AP, float *x, int incx)
```

performs one of the matrix-vector operations

\[ x = \text{op}(A) \ast x, \]

where \( \text{op}(A) = A \text { or } A^T \),

\( x \) is an \( n \)-element single-precision vector, and \( A \) is an \( n \times n \), unit or non-unit, upper or lower, triangular matrix consisting of single-precision elements.

**Input**

- `uplo` specifies whether the matrix \( A \) is an upper or lower triangular matrix.
  - If `uplo` == `'U'` or `'u'`, \( A \) is an upper triangular matrix.
  - If `uplo` == `'L'` or `'l'`, \( A \) is a lower triangular matrix.

- `trans` specifies \( \text{op}(A) \). If `trans` == `'N'` or `'n'`, \( \text{op}(A) = A \).
  - If `trans` == `'T'`, `'t'`, `'C'`, or `'c'`, \( \text{op}(A) = A^T \).

- `diag` specifies whether or not matrix \( A \) is unit triangular.
  - If `diag` == `'U'` or `'u'`, \( A \) is assumed to be unit triangular.
  - If `diag` == `'N'` or `'n'`, \( A \) is not assumed to be unit triangular.

- `n` specifies the number of rows and columns of the matrix \( A \); \( n \) must be at least zero. In the current implementation \( n \) must not exceed 4070.

- `AP` single-precision array with at least \( (n * (n + 1))/2 \) elements. If `uplo` == `'U'` or `'u'`, the array \( AP \) contains the upper triangular part of the symmetric matrix \( A \), packed sequentially, column by column; that is, if \( i <= j \), \( A[i, j] \) is stored in \( AP[i + (j * (j + 1))/2] \). If `uplo` == `'L'` or `'l'`, array \( AP \) contains the lower triangular part of the symmetric matrix \( A \), packed sequentially, column by column; that is, if \( i >= j \), \( A[i, j] \) is stored in \( AP[i + ((2 * n - j + 1) * j)/2] \).

- `x` single-precision array of length at least \( (1 + (n-1) \ast \text{abs}(\text{incx})) \).
  - On entry, \( x \) contains the source vector.
  - On exit, \( x \) is overwritten with the result vector.

- `incx` specifies the storage spacing for elements of \( x \); \( \text{incx} \) must not be zero.

**Output**

\( x \) updated according to \( x = \text{op}(A) \ast x \).

**Reference:** [http://www.netlib.org/blas/stpmv.f](http://www.netlib.org/blas/stpmv.f)
Error status for this function can be retrieved via `cublasGetError()`.  

**Error Status**  
<table>
<thead>
<tr>
<th>Status</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CUBLAS_STATUS_NOT_INITIALIZED</td>
<td>if CUBLAS library was not initialized</td>
</tr>
<tr>
<td>CUBLAS_STATUS_INVALID_VALUE</td>
<td>if <code>incx == 0</code>, <code>n &lt; 0</code>, or <code>n &gt; 4070</code></td>
</tr>
<tr>
<td>CUBLAS_STATUS_EXECUTION_FAILED</td>
<td>if function failed to launch on GPU</td>
</tr>
</tbody>
</table>

**Function `cublasStpsv()`**  

```c
void 
cublasStpsv (char uplo, char trans, char diag, int n, 
            const float *AP, float *X, int incx)
```

solves one of the systems of equations

$$
op(A) \cdot x = b,
\text{where } \op(A) = A \text{ or } \op(A) = A^T,$$

where

- $b$ and $x$ are $n$-element single-precision vectors,
- $A$ is an $n \times n$, unit or non-unit, upper or lower, triangular matrix.

No test for singularity or near-singularity is included in this function. Such tests must be performed before calling this function.

**Input**

- **uplo** specifies whether the matrix is an upper or lower triangular matrix. If `uplo == 'U'` or `'u'`, $A$ is an upper triangular matrix. If `uplo == 'L'` or `'l'`, $A$ is a lower triangular matrix.
- **trans** specifies $\op(A)$. If `trans == 'N'` or `'n'`, $\op(A) = A$. If `trans == 'T'`, `'t'`, `'C'`, or `'c'`, $\op(A) = A^T$.
- **diag** specifies whether $A$ is unit triangular. If `diag == 'U'` or `'u'`, $A$ is assumed to be unit triangular; that is, diagonal elements are not read and are assumed to be unity. If `diag == 'N'` or `'n'`, $A$ is not assumed to be unit triangular.
- **n** specifies the number of rows and columns of the matrix $A$; $n$ must be at least zero. In the current implementation $n$ must not exceed 4070.
CHAPTER 3 BLAS2 Functions

Input (continued)

$A_P$ single-precision array with at least $((n * (n + 1)) / 2)$ elements. If $\text{uplo} == 'U'$ or 'u', array $A_P$ contains the upper triangular matrix $A$, packed sequentially, column by column; that is, if $i <= j$, $A[i, j]$ is stored in $A_P[i + (j * (j + 1)) / 2]$. If $\text{uplo} == 'L'$ or 'l', array $A_P$ contains the lower triangular matrix $A$, packed sequentially, column by column; that is, if $i >= j$, $A[i, j]$ is stored in $A_P[i + ((2 * n - j + 1) * j) / 2]$. When $\text{diag} == 'U'$ or 'u', the diagonal elements of $A$ are not referenced and are assumed to be unity.

$x$ single-precision array of length at least $(1 + (n - 1) * \text{abs}(\text{incx}))$. On entry, $x$ contains the $n$-element right-hand side vector $b$. On exit, it is overwritten with the solution vector $x$.

$\text{incx}$ storage spacing between elements of $x$; $\text{incx}$ must not be zero.

Output

$x$ updated to contain the solution vector $x$ that solves $\text{op}(A) * x = b$.

Reference: http://www.netlib.org/blas/stpsv.f

Error status for this function can be retrieved via $\text{cublasGetError}()$.

Error Status

<table>
<thead>
<tr>
<th>Status</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CUBLAS_STATUS_NOT_INITIALIZED</td>
<td>if CUBLAS library was not initialized</td>
</tr>
<tr>
<td>CUBLAS_STATUS_INVALID_VALUE</td>
<td>if $\text{incx} == 0, n &lt; 0, \text{or} n &gt; 4070$</td>
</tr>
<tr>
<td>CUBLAS_STATUS_EXECUTION_FAILED</td>
<td>if function failed to launch on GPU</td>
</tr>
</tbody>
</table>

Function $\text{cublasStrmv}()$

```c
void 
\text{cublasStrmv} (char uplo, char trans, char diag, int n, 
const float *A, int lda, float *x, int incx)
```

performs one of the matrix-vector operations

$x = \text{op}(A) * x,$

where $\text{op}(A) = A$ or $\text{op}(A) = A^T,$
x is an n-element single-precision vector, and A is an n×n, unit or non-unit, upper or lower, triangular matrix consisting of single-precision elements.

Input

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>uplo</td>
<td>specifies whether the matrix A is an upper or lower triangular matrix. If uplo == 'U' or 'u', A is an upper triangular matrix. If uplo == 'L' or 'l', A is an lower triangular matrix.</td>
</tr>
<tr>
<td>trans</td>
<td>specifies op(A). If trans == 'N' or 'n', op(A) = A. If trans == 'T', 't', 'C', or 'c', op(A) = A^T.</td>
</tr>
<tr>
<td>diag</td>
<td>specifies whether or not A is a unit triangular matrix. If diag == 'U' or 'u', A is assumed to be unit triangular. If diag == 'N' or 'n', A is not assumed to be unit triangular.</td>
</tr>
<tr>
<td>n</td>
<td>specifies the number of rows and columns of the matrix A; n must be at least zero. In the current implementation, n must not exceed 4070.</td>
</tr>
<tr>
<td>A</td>
<td>single-precision array of dimensions (lda, n). If uplo == 'U' or 'u', the leading n×n upper triangular part of the array A must contain the upper triangular matrix, and the strictly lower triangular part of A is not referenced. If uplo == 'L' or 'l', the leading n×n lower triangular part of the array A must contain the lower triangular matrix, and the strictly upper triangular part of A is not referenced. When diag == 'U' or 'u', the diagonal elements of A are not referenced either, but are assumed to be unity.</td>
</tr>
<tr>
<td>lda</td>
<td>leading dimension of A; lda must be at least max(1, n).</td>
</tr>
<tr>
<td>x</td>
<td>single-precision array of length at least (1 + (n - 1) * abs(incx)). On entry, x contains the source vector. On exit, x is overwritten with the result vector.</td>
</tr>
<tr>
<td>incx</td>
<td>the storage spacing between elements of x; incx must not be zero.</td>
</tr>
</tbody>
</table>

Output

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>x</td>
<td>updated according to x = op(A) * x.</td>
</tr>
</tbody>
</table>

Reference: [http://www.netlib.org/blas/strmv.f](http://www.netlib.org/blas/strmv.f)

Error status for this function can be retrieved via `cublasGetError()`. Error Status

<table>
<thead>
<tr>
<th>Error Code</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CUBLAS_STATUS_NOT_INITIALIZED</td>
<td>if CUBLAS library was not initialized</td>
</tr>
<tr>
<td>CUBLAS_STATUS_INVALID_VALUE</td>
<td>if incx == 0, n &lt; 0, or n &gt; 4070</td>
</tr>
<tr>
<td>CUBLAS_STATUS_EXECUTION_FAILED</td>
<td>if function failed to launch on GPU</td>
</tr>
</tbody>
</table>
Function cublasStrsv()

```c
void
cublasStrsv (char uplo, char trans, char diag, int n,
            const float *A, int lda, float *x, int incx)
```

solves a system of equations

$$\text{op}(A) \cdot x = b,$$

where $$\text{op}(A) = A$$ or $$\text{op}(A) = A^T,$$

$b$ and $x$ are $n$-element single-precision vectors, and $A$ is an $n \times n$, unit or non-unit, upper or lower, triangular matrix consisting of single-precision elements. Matrix $A$ is stored in column-major format, and $lda$ is the leading dimension of the two-dimensional array containing $A$.

No test for singularity or near-singularity is included in this function. Such tests must be performed before calling this function.

Input

- **uplo** specifies whether the matrix data is stored in the upper or the lower triangular part of array $A$. If $\text{uplo} = 'U'$ or $'u'$, only the upper triangular part of $A$ may be referenced. If $\text{uplo} = 'L'$ or $'l'$, only the lower triangular part of $A$ may be referenced.

- **trans** specifies $\text{op}(A)$. If $\text{trans} = 'N'$ or $'n'$, $\text{op}(A) = A$. If $\text{trans} = 'T'$, 't', 'C', or 'c', $\text{op}(A) = A^T$.

- **diag** specifies whether or not $A$ is a unit triangular matrix. If $\text{diag} = 'U'$ or $'u'$, $A$ is assumed to be unit triangular. If $\text{diag} = 'N'$ or $'n'$, $A$ is not assumed to be unit triangular.

- **n** specifies the number of rows and columns of the matrix $A$; $n$ must be at least zero. In the current implementation, $n$ must not exceed 4070.

- **A** single-precision array of dimensions $(lda, n)$. If $\text{uplo} = 'U'$ or $'u'$, $A$ contains the upper triangular part of the symmetric matrix, and the strictly lower triangular part is not referenced. If $\text{uplo} = 'L'$ or $'l'$, $A$ contains the lower triangular part of the symmetric matrix, and the strictly upper triangular part is not referenced.

- **lda** leading dimension of the two-dimensional array containing $A$; $lda$ must be at least $\max(1, n)$.

- **x** single-precision array of length at least $(1 + (n - 1) \times \text{abs}(\text{incx}))$. On entry, $x$ contains the $n$-element, right-hand-side vector $b$. On exit, it is overwritten with the solution vector $x$.

- **incx** the storage spacing between elements of $x$; $\text{incx}$ must not be zero.
CUDA

CUBLAS Library

Output

\begin{align*}
\mathbf{x} \quad & \text{updated to contain the solution vector } \mathbf{x} \text{ that solves } \mathbf{op}(\mathbf{A}) \mathbf{x} = \mathbf{b}.
\end{align*}

Reference: http://www.netlib.org/blas/strsv.f

Error status for this function can be retrieved via \texttt{cublasGetError()}.  

Error Status

\begin{itemize}
  \item \texttt{CUBLAS_STATUS_NOT_INITIALIZED} if CUBLAS library was not initialized
  \item \texttt{CUBLAS_STATUS_INVALID_VALUE} if \texttt{incx} \(= 0\), \texttt{n} \(< 0\), or \texttt{n} \(> 4070\)
  \item \texttt{CUBLAS_STATUS_EXECUTION_FAILED} if function failed to launch on GPU
\end{itemize}

---

Single-Precision Complex BLAS2 Functions

These functions have not been implemented yet.
CHAPTER 3

BLAS2 Functions

Double-Precision BLAS2 Functions

Note: Double-precision functions are only supported on GPUs with double-precision hardware.

The double-precision BLAS2 functions are as follows:
- “Function cublasDgemv()” on page 77
- “Function cublasDger()” on page 78
- “Function cublasDsyr()” on page 79
- “Function cublasDtrsv()” on page 81

Function cublasDgemv()

```c
void
cublasDgemv (char trans, int m, int n, double alpha,
const double *A, int lda, const double *x,
int incx, double beta, double *y, int incy)
```

performs one of the matrix-vector operations

\[
y = \alpha \cdot \text{op}(A) \cdot x + \beta \cdot y,
\]

where \( \text{op}(A) = A \) or \( \text{op}(A) = A^T \),

\( \alpha \) and \( \beta \) are double-precision scalars, and \( x \) and \( y \) are double-precision vectors. \( A \) is an \( m \times n \) matrix consisting of double-precision elements. Matrix \( A \) is stored in column-major format, and \( \text{lda} \) is the leading dimension of the two-dimensional array in which \( A \) is stored.

**Input**

- \( \text{trans} \) specifies \( \text{op}(A) \). If \( \text{trans} == 'N' \) or \( 'n' \), \( \text{op}(A) = A \).
  - If \( \text{trans} == 'T', 't', 'C', \) or \( 'c' \), \( \text{op}(A) = A^T \).
- \( m \) specifies the number of rows of matrix \( A \); \( m \) must be at least zero.
- \( n \) specifies the number of columns of matrix \( A \); \( n \) must be at least zero.
- \( \alpha \) double-precision scalar multiplier applied to \( \text{op}(A) \).
- \( A \) double-precision array of dimensions (\( \text{lda}, n \)) if \( \text{trans} == 'N' \) or \( 'n' \), of dimensions (\( \text{lda}, m \)) otherwise; \( \text{lda} \) must be at least \( \max(1, m) \) if \( \text{trans} == 'N' \) or \( 'n' \) and at least \( \max(1, n) \) otherwise.
- \( \text{lda} \) leading dimension of two-dimensional array used to store matrix \( A \).
CUDA

CUBLAS Library

Input (continued)

\[ x \text{ double-precision array of length at least } (1 + (n-1) \cdot \text{abs}(\text{incx})) \text{ if } \text{trans} == 'N' \text{ or } 'n', \text{ else at least } (1 + (m-1) \cdot \text{abs}(\text{incx})). \]

\text{incx} \text{ specifies the storage spacing for elements of } x; \text{ incx must not be zero.}

\text{beta} \text{ double-precision scalar multiplier applied to vector } y. \text{ If } \text{beta} \text{ is zero, }
\\text{y is not read.}

\[ y \text{ double-precision array of length at least } (1 + (m-1) \cdot \text{abs}(\text{incy})) \text{ if } \text{trans} == 'N' \text{ or } 'n', \text{ else at least } (1 + (n-1) \cdot \text{abs}(\text{incy})). \]

\text{incy} \text{ the storage spacing between elements of } y; \text{ incy must not be zero.}

Output

\[ y \text{ updated according to } y = \text{alpha} \cdot \text{op}(A) \cdot x + \text{beta} \cdot y. \]

Reference: [http://www.netlib.org/blas/dgemv.f](http://www.netlib.org/blas/dgemv.f)

Error status for this function can be retrieved via \textit{cublasGetError}().

Error Status

\begin{align*}
\text{CUBLAS_STATUS_NOT_INITIALIZED} & \text{ if CUBLAS library was not initialized} \\
\text{CUBLAS_STATUS_INVALID_VALUE} & \text{ if } m < 0, n < 0, \text{incx} == 0, \text{ or } \text{incy} == 0 \\
\text{CUBLAS_STATUS_ARCH_MISMATCH} & \text{ if function invoked on device that } \\
& \text{does not support double precision} \\
\text{CUBLAS_STATUS_EXECUTION_FAILED} & \text{ if function failed to launch on GPU}
\end{align*}

Function \textit{cublasDger()}

\begin{verbatim}
void
cublasDger (int m, int n, double alpha, const double *x, 
int incx, const double *y, int incy, 
double *A, int lda)
\end{verbatim}

performs the symmetric rank 1 operation

\[ A = \alpha \cdot x \cdot y^T + A, \]

where \alpha is a double-precision scalar, \( x \) is an \( m \)-element double-precision vector, \( y \) is an \( n \)-element double-precision vector, and \( A \) is an \( m \times n \) matrix consisting of double-precision elements. Matrix \( A \) is stored
in column-major format, and \( \text{lda} \) is the leading dimension of the two-dimensional array used to store \( A \).

**Input**

- \( m \) specifies the number of rows of the matrix \( A \); \( m \) must be at least zero.
- \( n \) specifies the number of columns of matrix \( A \); \( n \) must be at least zero.
- \( \alpha \) double-precision scalar multiplier applied to \( x \star y^T \).
- \( x \) double-precision array of length at least \((1 + \text{abs}(\text{incx})) \).
- \( \text{incx} \) the storage spacing between elements of \( x \); \( \text{incx} \) must not be zero.
- \( y \) double-precision array of length at least \((1 + \text{abs}(\text{incy})) \).
- \( \text{incy} \) the storage spacing between elements of \( y \); \( \text{incy} \) must not be zero.
- \( A \) double-precision array of dimensions \((\text{lda}, n)\).
- \( \text{lda} \) leading dimension of two-dimensional array used to store matrix \( A \).

**Output**

- \( A \) updated according to \( A = \alpha \star x \star y^T + A \).

**Reference:** [http://www.netlib.org/blas/dger.f](http://www.netlib.org/blas/dger.f)

Error status for this function can be retrieved via \texttt{cublasGetError()}.

**Error Status**

- \texttt{CUBLAS_STATUS_NOT_INITIALIZED} if CUBLAS library was not initialized
- \texttt{CUBLAS_STATUS_INVALID_VALUE} if \( m < 0, n < 0, \text{incx} = 0, \text{incy} = 0 \)
- \texttt{CUBLAS_STATUS_ARCH_MISMATCH} if function invoked on device that does not support double precision
- \texttt{CUBLAS_STATUS_EXECUTION_FAILED} if function failed to launch on GPU

**Function cublasDsyr()**

```c
void
  cublasDsyr (char uplo, int n, double alpha,
              const double *x, int incx, double *A,
              int lda)
```

performs the symmetric rank 1 operation

\[
A = \alpha \star x \star x^T + A,
\]
where \( \alpha \) is a double-precision scalar, \( x \) is an \( n \)-element double-precision vector, and \( A \) is an \( n \times n \) symmetric matrix consisting of double-precision elements. \( A \) is stored in column-major format, and \( \text{lda} \) is the leading dimension of the two-dimensional array containing \( A \).

**Input**

- \( \text{uplo} \) specifies whether the matrix data is stored in the upper or the lower triangular part of array \( A \). If \( \text{uplo} = 'U' \) or \( 'u' \), only the upper triangular part of \( A \) is referenced. If \( \text{uplo} = 'L' \) or \( 'l' \), only the lower triangular part of \( A \) is referenced.
- \( n \) is the number of rows and columns of matrix \( A; n \) must be at least zero.
- \( \alpha \) is a double-precision scalar multiplier applied to \( x \).
- \( A \) is a double-precision array of length at least \( 1 + (n-1) \times \text{abs}(\text{incx}) \).
- \( \text{incx} \) is the storage spacing between elements of \( x \); \( \text{incx} \) must not be zero.
- \( \text{lda} \) is the leading dimension of the two-dimensional array containing \( A \); \( \text{lda} \) must be at least \( \max(1, n) \).

**Output**

- \( A \) is updated according to \( A = \alpha \times x \times x^T + A \).

**Reference:** [http://www.netlib.org/blas/dsyr.f](http://www.netlib.org/blas/dsyr.f)

**Error Status**

- **CUBLAS_STATUS_NOT_INITIALIZED** if CUBLAS library was not initialized
- **CUBLAS_STATUS_INVALID_VALUE** if \( n < 0 \) or \( \text{incx} == 0 \)
- **CUBLAS_STATUS_ARCH_MISMATCH** if function invoked on device that does not support double precision
- **CUBLAS_STATUS_EXECUTION_FAILED** if function failed to launch on GPU
Function cublasDtrsv()

```c
void
cublasDtrsv(char uplo, char trans, char diag, int n,
const double *A, int lda, double *x, 
int incx)
```
solves a system of equations

```latex
\text{op}(A) \times x = b,
\text{where } \text{op}(A) = A \text{ or } \text{op}(A) = A^T,
```

$b$ and $x$ are $n$-element double-precision vectors, and $A$ is an $n \times n$, unit or non-unit, upper or lower, triangular matrix consisting of double-precision elements. Matrix $A$ is stored in column-major format, and $\text{lda}$ is the leading dimension of the two-dimensional array containing $A$.

No test for singularity or near-singularity is included in this function. Such tests must be performed before calling this function.

**Input**

- **uplo** specifies whether the matrix data is stored in the upper or the lower triangular part of array $A$. If $\text{uplo} == 'U'$ or $'u'$, only the upper triangular part of $A$ may be referenced. If $\text{uplo} == 'L'$ or $'l'$, only the lower triangular part of $A$ may be referenced.

- **trans** specifies $\text{op}(A)$. If $\text{trans} == 'N'$ or $'n'$, $\text{op}(A) = A$. If $\text{trans} == 'T'$, $'t'$, $'C'$, or $'c'$, $\text{op}(A) = A^T$.

- **diag** specifies whether or not $A$ is a unit triangular matrix. If $\text{diag} == 'U'$ or $'u'$, $A$ is assumed to be unit triangular. If $\text{diag} == 'N'$ or $'n'$, $A$ is not assumed to be unit triangular.

- **n** specifies the number of rows and columns of the matrix $A$; $n$ must be at least zero. In the current implementation, $n$ must not exceed 2040.

- **A** double-precision array of dimensions ($\text{lda}$, $n$). If $\text{uplo} == 'U'$ or $'u'$, $A$ contains the upper triangular part of the symmetric matrix, and the strictly lower triangular part is not referenced. If $\text{uplo} == 'L'$ or $'l'$, $A$ contains the lower triangular part of the symmetric matrix, and the strictly upper triangular part is not referenced.

- **lda** leading dimension of the two-dimensional array containing $A$; $\text{lda}$ must be at least $\max(1, n)$. 
Input (continued)

\( x \)  
double-precision array of length at least \((1+(n-1) \times \text{abs}(\text{incx}))\).  
On entry, \( x \) contains the \( n \)-element, right-hand-side vector \( b \).  
On exit, it is overwritten with the solution vector \( x \).

\( \text{incx} \)  
the storage spacing between elements of \( x \); \( \text{incx} \) must not be zero.

Output

\( x \)  
updated to contain the solution vector \( x \) that solves \( \text{op}(A) * x = b \).

Reference: [http://www.netlib.org/blas/dtrsv.f](http://www.netlib.org/blas/dtrsv.f)

Error status for this function can be retrieved via `cublasGetError()`.

Error Status

- `CUBLAS_STATUS_NOT_INITIALIZED` if CUBLAS library was not initialized
- `CUBLAS_STATUS_INVALID_VALUE` if \( \text{incx} = 0 \), \( n < 0 \), or \( n > 2040 \)
- `CUBLAS_STATUS_ARCH_MISMATCH` if function invoked on device that does not support double precision
- `CUBLAS_STATUS_EXECUTION_FAILED` if function failed to launch on GPU

---

**Double-Precision Complex BLAS2 functions**

These functions have not been implemented yet.
Level 3 Basic Linear Algebra Subprograms (BLAS3) perform matrix-matrix operations. The CUBLAS implementations are described in the following sections:

- “Single-Precision BLAS3 Functions” on page 84
- “Single-Precision Complex BLAS3 Functions” on page 95
- “Double-Precision BLAS3 Functions” on page 97
- “Double-Precision Complex BLAS3 Functions” on page 109
Single-Precision BLAS3 Functions

The single-precision BLAS3 functions are listed below:

- “Function cublasSgemm()” on page 84
- “Function cublasSsymm()” on page 86
- “Function cublasSsyrk()” on page 88
- “Function cublasSsyr2k()” on page 89
- “Function cublasStrmm()” on page 91
- “Function cublasStrsm()” on page 93

Function cublasSgemm()

```c
void
cublasSgemm (char transa, char transb, int m, int n,
int k, float alpha, const float *A, int lda,
const float *B, int ldb, float beta,
float *C, int ldc)
```

computes the product of matrix A and matrix B, multiplies the result by scalar alpha, and adds the sum to the product of matrix C and scalar beta. It performs one of the matrix-matrix operations:

\[
C = \alpha \cdot \text{op}(A) \cdot \text{op}(B) + \beta \cdot C,
\]

where \( \text{op}(X) = X \) or \( \text{op}(X) = X^T \),

and \( \alpha \) and \( \beta \) are single-precision scalars. A, B, and C are matrices consisting of single-precision elements, with \( \text{op}(A) \) an \( m \times k \) matrix, \( \text{op}(B) \) a \( k \times n \) matrix, and C an \( m \times n \) matrix. Matrices A, B, and C are stored in column-major format, and \( \text{lda}, \text{ldb}, \) and \( \text{ldc} \) are the leading dimensions of the two-dimensional arrays containing A, B, and C.

Input

- `transa` specifies \( \text{op}(A) \). If `transa` == 'N' or 'n', \( \text{op}(A) = A \).
  - If `transa` == 'T', 't', 'C', or 'c', \( \text{op}(A) = A^T \).
- `transb` specifies \( \text{op}(B) \). If `transb` == 'N' or 'n', \( \text{op}(B) = B \).
  - If `transb` == 'T', 't', 'C', or 'c', \( \text{op}(B) = B^T \).
- `m` number of rows of matrix \( \text{op}(A) \) and rows of matrix C; \( m \) must be at least zero.
CHAPTER 4
BLAS3 Functions

Input (continued)

n  number of columns of matrix $\text{op}(B)$ and number of columns of $C$; $n$ must be at least zero.
k  number of columns of matrix $\text{op}(A)$ and number of rows of $\text{op}(B)$; $k$ must be at least zero.
alpha single-precision scalar multiplier applied to $\text{op}(A) * \text{op}(B)$.
A  single-precision array of dimensions $(\text{lda}, k)$ if $\text{transa} == 'N'$ or '$n$', and of dimensions $(\text{lda}, m)$ otherwise. If $\text{transa} == 'N'$ or '$n$', $\text{lda}$ must be at least $\max(1, m)$; otherwise, $\text{lda}$ must be at least $\max(1, k)$.
lda leading dimension of two-dimensional array used to store matrix $A$.
B  single-precision array of dimensions $(\text{ldb}, n)$ if $\text{transb} == 'N'$ or '$n$', and of dimensions $(\text{ldb}, k)$ otherwise. If $\text{transb} == 'N'$ or '$n$', $\text{ldb}$ must be at least $\max(1, k)$; otherwise, $\text{ldb}$ must be at least $\max(1, n)$.
ldb leading dimension of two-dimensional array used to store matrix $B$.
beta single-precision scalar multiplier applied to $C$. If zero, $C$ does not have to be a valid input.
C  single-precision array of dimensions $(\text{ldc}, n)$; $\text{ldc}$ must be at least $\max(1, m)$.
ldc leading dimension of two-dimensional array used to store matrix $C$.

Output

C  updated based on $C = \alpha * \text{op}(A) * \text{op}(B) + \beta * C$.

Reference: http://www.netlib.org/blas/sgemm.f

Error status for this function can be retrieved via $\text{cublasGetError()}$.

Error Status

- $\text{CUBLAS_STATUS_NOT_INITIALIZED}$ if CUBLAS library was not initialized
- $\text{CUBLAS_STATUS_INVALID_VALUE}$ if $m < 0$, $n < 0$, or $k < 0$
- $\text{CUBLAS_STATUS_EXECUTION_FAILED}$ if function failed to launch on GPU
Function `cublasSsymm()`

```c
void

cublasSsymm (char side, char uplo, int m, int n,
float alpha, const float *A, int lda,
const float *B, int ldb, float beta,
float *C, int ldc)
```

performs one of the matrix-matrix operations

\[
C = \alpha A \cdot B + \beta C \quad \text{or} \quad C = \alpha B \cdot A + \beta C,
\]

where \(\alpha\) and \(\beta\) are single-precision scalars, \(A\) is a symmetric matrix consisting of single-precision elements and is stored in either lower or upper storage mode. \(B\) and \(C\) are \(m \times n\) matrices consisting of single-precision elements.

**Input**

- **side** specifies whether the symmetric matrix \(A\) appears on the left-hand side or right-hand side of matrix \(B\).
  - If `side` == `'L'` or `'l'`, \(C = \alpha A \cdot B + \beta C\).
  - If `side` == `'R'` or `'r'`, \(C = \alpha B \cdot A + \beta C\).

- **uplo** specifies whether the symmetric matrix \(A\) is stored in upper or lower storage mode. If `uplo` == `'U'` or `'u'`, only the upper triangular part of the symmetric matrix is referenced, and the elements of the strictly lower triangular part are inferred from those in the upper triangular part. If `uplo` == `'L'` or `'l'`, only the lower triangular part of the symmetric matrix is referenced, and the elements of the strictly upper triangular part are inferred from those in the lower triangular part.

- **m** specifies the number of rows of matrix \(C\), and the number of rows of matrix \(B\). It also specifies the dimensions of symmetric matrix \(A\) when `side` == `'L'` or `'l'`; \(m\) must be at least zero.

- **n** specifies the number of columns of matrix \(C\), and the number of columns of matrix \(B\). It also specifies the dimensions of symmetric matrix \(A\) when `side` == `'R'` or `'r'`; \(n\) must be at least zero.

- **alpha** single-precision scalar multiplier applied to \(A \cdot B\) or \(B \cdot A\).
CHAPTER 4 BLAS3 Functions

Input (continued)

A single-precision array of dimensions (lda, ka), where ka is m when side == 'L' or 'l' and is n otherwise. If side == 'L' or 'l', the leading m×m part of array A must contain the symmetric matrix, such that when uplo == 'U' or 'u', the leading m×m part stores the upper triangular part of the symmetric matrix, and the strictly lower triangular part of A is not referenced; and when uplo == 'L' or 'l', the leading m×m part stores the lower triangular part of the symmetric matrix and the strictly upper triangular part is not referenced. If side == 'R' or 'r', the leading n×n part of array A must contain the symmetric matrix, such that when uplo == 'U' or 'u', the leading n×n part stores the upper triangular part of the symmetric matrix and the strictly lower triangular part of A is not referenced; and when uplo == 'L' or 'l', the leading n×n part stores the lower triangular part of the symmetric matrix and the strictly upper triangular part is not referenced.

lda leading dimension of A. When side == 'L' or 'l', it must be at least max(1, m) and at least max(1, n) otherwise.

B single-precision array of dimensions (ldb, n). On entry, the leading m×n part of the array contains the matrix B.

ldb leading dimension of B; ldb must be at least max(1, m).

beta single-precision scalar multiplier applied to C. If beta is zero, C does not have to be a valid input.

C single-precision array of dimensions (ldc, n).

ldc leading dimension of C; ldc must be at least max(1, m).

Output

C updated according to C = alpha * A * B + beta * C or C = alpha * B * A + beta * C.

Reference: http://www.netlib.org/blas/ssymm

Error status for this function can be retrieved via cublasGetError().

Error Status

CUBLAS_STATUS_NOT_INITIALIZED if CUBLAS library was not initialized

CUBLAS_STATUS_INVALID_VALUE if m < 0 or n < 0

CUBLAS_STATUS_EXECUTION_FAILED if function failed to launch on GPU
Function cublasSsyrk()

```c
void
cublasSsyrk (char uplo, char trans, int n, int k,
            float alpha, const float *A, int lda,
            float beta, float *C, int ldc)
```

performs one of the symmetric rank k operations

\[ C = \alpha \cdot A \cdot A^T + \beta \cdot C \quad \text{or} \quad C = \alpha \cdot A^T \cdot A + \beta \cdot C, \]

where \( \alpha \) and \( \beta \) are single-precision scalars. \( C \) is an \( n \times n \) symmetric matrix consisting of single-precision elements and is stored in either lower or upper storage mode. \( A \) is a matrix consisting of single-precision elements with dimensions of \( n \times k \) in the first case, and \( k \times n \) in the second case.

Input

- \( \text{uplo} \): specifies whether the symmetric matrix \( C \) is stored in upper or lower storage mode. If \( \text{uplo} == 'U' \) or \( 'u' \), only the upper triangular part of the symmetric matrix is referenced, and the elements of the strictly lower triangular part are inferred from those in the upper triangular part. If \( \text{uplo} == 'L' \) or \( 'l' \), only the lower triangular part of the symmetric matrix is referenced, and the elements of the strictly upper triangular part are inferred from those in the lower triangular part.

- \( \text{trans} \): specifies the operation to be performed. If \( \text{trans} == 'N' \) or \( 'n' \), \( C = \alpha \cdot A \cdot A^T + \beta \cdot C \). If \( \text{trans} == 'T', 't', 'C' \), or \( 'c' \), \( C = \alpha \cdot A^T \cdot A + \beta \cdot C \).

- \( n \): specifies the number of rows and the number columns of matrix \( C \). If \( \text{trans} == 'N' \) or \( 'n' \), \( n \) specifies the number of rows of matrix \( A \). If \( \text{trans} == 'T', 't', 'C' \), or \( 'c' \), \( n \) specifies the number of columns of matrix \( A \); \( n \) must be at least zero.

- \( k \): If \( \text{trans} == 'N' \) or \( 'n' \), \( k \) specifies the number of columns of matrix \( A \). If \( \text{trans} == 'T', 't', 'C' \), or \( 'c' \), \( k \) specifies the number of rows of matrix \( A \); \( k \) must be at least zero.

- \( \text{alpha} \): single-precision scalar multiplier applied to \( A \cdot A^T \) or \( A^T \cdot A \).

- \( A \): single-precision array of dimensions \((\text{lda}, \text{ka})\), where \( \text{ka} \) is \( k \) when \( \text{trans} == 'N' \) or \( 'n' \), and is \( n \) otherwise. When \( \text{trans} == 'N' \) or \( 'n' \), the leading \( n \times k \) part of array \( A \) contains the matrix \( A \); otherwise, the leading \( k \times n \) part of the array contains the matrix \( A \).

- \( \text{lda} \): leading dimension of \( A \). When \( \text{trans} == 'N' \) or \( 'n' \), \( \text{lda} \) must be at least \( \max(1, n) \). Otherwise \( \text{lda} \) must be at least \( \max(1, k) \).
CHAPTER 4  BLAS3 Functions

Input (continued)

**beta**
- single-precision scalar multiplier applied to C.
  - If beta is zero, C is not read.

**C**
- single-precision array of dimensions (ldc, n). If uplo == 'U' or 'u',
  the leading n×n triangular part of the array C must contain the upper
  triangular part of the symmetric matrix C, and the strictly lower
  triangular part of C is not referenced. On exit, the upper triangular part
  of C is overwritten by the upper triangular part of the updated matrix.
  If uplo == 'L' or 'l', the leading n×n triangular part of the array C
  must contain the lower triangular part of the symmetric matrix C, and
  the strictly upper triangular part of C is not referenced. On exit, the
  lower triangular part of C is overwritten by the lower triangular part
  of the updated matrix.

**ldc**
- leading dimension of C; ldc must be at least max(1, n).

Output

**C**
- updated according to C = alpha * A * A^T + beta * C or
  C = alpha * A^T * A + beta * C.

Reference: [http://www.netlib.org/blas/ssyrk.f](http://www.netlib.org/blas/ssyrk.f)

Error status for this function can be retrieved via `cublasGetError()`.

**Error Status**

- **CUBLAS_STATUS_NOT_INITIALIZED** if CUBLAS library was not initialized
- **CUBLAS_STATUS_INVALID_VALUE** if n < 0 or k < 0
- **CUBLAS_STATUS_EXECUTION_FAILED** if function failed to launch on GPU

**Function cublasSsyr2k()**

```c
void cublasSsyr2k (char uplo, char trans, int n, int k,
  float alpha, const float *A, int lda,
  const float *B, int ldb, float beta,
  float *C, int ldc)
```

performs one of the symmetric rank 2k operations

\[ C = \alpha A \cdot A^T + \alpha B \cdot B^T + \beta C \] or
\[ C = \alpha A^T \cdot A + \alpha B \cdot B^T + \beta C, \]

where alpha and beta are single-precision scalars. C is an n×n
symmetric matrix consisting of single-precision elements and is stored
in either lower or upper storage mode. A and B are matrices consisting of single-precision elements with dimension of \( n \times k \) in the first case, and \( k \times n \) in the second case.

**Input**

- **uplo** specifies whether the symmetric matrix \( C \) is stored in upper or lower storage mode. If \( \text{uplo} == \'U' \) or \('u'\), only the upper triangular part of the symmetric matrix is referenced, and the elements of the strictly lower triangular part are inferred from those in the upper triangular part. If \( \text{uplo} == \'L' \) or \('l'\), only the lower triangular part of the symmetric matrix is referenced, and the elements of the strictly upper triangular part are inferred from those in the lower triangular part.

- **trans** specifies the operation to be performed. If \( \text{trans} == \'N' \) or \('n'\), \( \begin{align*} C &= \text{alpha} \times A \times B^T + \text{alpha} \times B \times A^T + \text{beta} \times C. \end{align*} \) If \( \text{trans} == \'T' \), \('t'\), \('C'\), or \('c'\), \( \begin{align*} C &= \text{alpha} \times A^T \times B + \text{alpha} \times B^T \times A + \text{beta} \times C. \end{align*} \)

- **n** specifies the number of rows and the number columns of matrix \( C \). If \( \text{trans} == \'N' \) or \('n'\), \( n \) specifies the number of rows of matrix \( A \). If \( \text{trans} == \'T' \), \('t'\), \('C'\), or \('c'\), \( n \) specifies the number of columns of matrix \( A \); \( n \) must be at least zero.

- **k** If \( \text{trans} == \'N' \) or \('n'\), \( k \) specifies the number of columns of matrix \( A \). If \( \text{trans} == \'T' \), \('t'\), \('C'\), or \('c'\), \( k \) specifies the number of rows of matrix \( A \); \( k \) must be at least zero.

- **alpha** single-precision scalar multiplier.

- **A** single-precision array of dimensions \((\text{lda, ka})\), where \( \text{ka} = k \) when \( \text{trans} == \'N' \) or \('n'\), and is \( n \) otherwise. When \( \text{trans} == \'N' \) or \('n'\), the leading \( n \times k \) part of array \( A \) must contain the matrix \( A \), otherwise the leading \( k \times n \) part of the array must contain the matrix \( A \).

- **lda** leading dimension of \( A \). When \( \text{trans} == \'N' \) or \('n'\), \( \text{lda} \) must be at least \( \max(1,n) \). Otherwise \( \text{lda} \) must be at least \( \max(1,k) \).

- **B** single-precision array of dimensions \((\text{ldb, kb})\), where \( \text{kb} = k \) when \( \text{trans} == \'N' \) or \('n'\), and \( k = n \) otherwise. When \( \text{trans} == \'N' \) or \('n'\), the leading \( n \times k \) part of array \( B \) must contain the matrix \( B \), otherwise the leading \( k \times n \) part of the array must contain the matrix \( B \).

- **ldb** leading dimension of \( B \). When \( \text{trans} == \'N' \) or \('n'\), \( \text{ldb} \) must be at least \( \max(1,n) \). Otherwise \( \text{ldb} \) must be at least \( \max(1,k) \).

- **beta** single-precision scalar multiplier applied to \( C \). If \( \text{beta} \) is zero, \( C \) does not have to be a valid input.
CHAPTER 4
BLAS3 Functions

Input (continued)

C  single-precision array of dimensions (ldc,n). If uplo == 'U' or 'u',
the leading \( n \times n \) triangular part of the array \( C \) must contain the upper
triangular part of the symmetric matrix \( C \), and the strictly lower
triangular part of \( C \) is not referenced. On exit, the upper triangular part
of \( C \) is overwritten by the upper triangular part of the updated matrix.
If uplo == 'L' or 'l', the leading \( n \times n \) triangular part of the array \( C \)
must contain the lower triangular part of the symmetric matrix \( C \), and
the strictly upper triangular part of \( C \) is not referenced. On exit, the
lower triangular part of \( C \) is overwritten by the lower triangular part
of the updated matrix.

ldc  leading dimension of \( C \); ldc must be at least \( \max(1,n) \).

Output

C  updated according to
    \[
    C = \alpha A \cdot B^T + \alpha B \cdot A^T + \beta C \quad \text{or} \\
    C = \alpha A^T \cdot B + \alpha B^T \cdot A + \beta C.
    \]

Reference:  [http://www.netlib.org/blas/sssyr2k.f](http://www.netlib.org/blas/sssyr2k.f)

Error status for this function can be retrieved via `cublasGetError()`.

Error Status

<table>
<thead>
<tr>
<th>Code</th>
<th>Description</th>
</tr>
</thead>
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<tr>
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</tr>
<tr>
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</tr>
</tbody>
</table>

Function `cublasStrmm()`

```c
void
cublasStrmm (char side, char uplo, char transa, 
char diag, int m, int n, float alpha, 
const float *A, int lda, const float *B, 
int ldb)
```

performs one of the matrix-matrix operations

\[
B = \alpha \circ \text{op} (A) \cdot B \quad \text{or} \quad B = \alpha B \cdot \text{op}(A),
\]

where \( \text{op}(A) = A \text{ or } \text{op}(A) = A^T \).

\( \alpha \) is a single-precision scalar, \( B \) is an \( m \times n \) matrix consisting of
single-precision elements, and \( A \) is a unit or non-unit, upper or lower
triangular matrix consisting of single-precision elements.
Matrices $A$ and $B$ are stored in column-major format, and $\text{lda}$ and $\text{ldb}$ are the leading dimensions of the two-dimensional arrays that contain $A$ and $B$, respectively.

**Input**

- **side** specifies whether $\text{op}(A)$ multiplies $B$ from the left or right. If $\text{side} == 'L'$ or 'l', $B = \text{alpha} \times \text{op}(A) \times B$.
  
  If $\text{side} == 'R'$ or 'r', $B = \text{alpha} \times B \times \text{op}(A)$.

- **uplo** specifies whether the matrix $A$ is an upper or lower triangular matrix. If $\text{uplo} == 'U'$ or 'u', $A$ is an upper triangular matrix.
  
  If $\text{uplo} == 'L'$ or 'l', $A$ is a lower triangular matrix.

- **transa** specifies the form of $\text{op}(A)$ to be used in the matrix multiplication. If $\text{transa} == 'N'$ or 'n', $\text{op}(A) = A$.
  
  If $\text{transa} == 'T'$, 't', 'C', or 'c', $\text{op}(A) = A^T$.

- **diag** specifies whether or not $A$ is a unit triangular matrix. If $\text{diag} == 'U'$ or 'u', $A$ is assumed to be unit triangular. If $\text{diag} == 'N'$ or 'n', $A$ is not assumed to be unit triangular.

- **m** the number of rows of matrix $B$; $m$ must be at least zero.

- **n** the number of columns of matrix $B$; $n$ must be at least zero.

- **alpha** single-precision scalar multiplier applied to $\text{op}(A) \times B$ or $B \times \text{op}(A)$, respectively. If $\text{alpha}$ is zero, no accesses are made to matrix $A$, and no read accesses are made to matrix $B$.

- **A** single-precision array of dimensions $(\text{lda}, k)$. If $\text{side} == 'L'$ or 'l', $k = m$. If $\text{side} == 'R'$ or 'r', $k = n$. If $\text{uplo} == 'U'$ or 'u', the leading $k \times k$ upper triangular part of the array $A$ must contain the upper triangular matrix, and the strictly lower triangular part of $A$ is not referenced. If $\text{uplo} == 'L'$ or 'l', the leading $k \times k$ lower triangular part of the array $A$ must contain the lower triangular matrix, and the strictly upper triangular part of $A$ is not referenced. When $\text{diag} == 'U'$ or 'u', the diagonal elements of $A$ are not referenced and are assumed to be unity.

- **lda** leading dimension of $A$. When $\text{side} == 'L'$ or 'l', it must be at least $\max(1, m)$ and at least $\max(1, n)$ otherwise.

- **B** single-precision array of dimensions $(\text{ldb}, n)$. On entry, the leading $m \times n$ part of the array contains the matrix $B$. It is overwritten with the transformed matrix on exit.

- **ldb** leading dimension of $B$; $\text{ldb}$ must be at least $\max(1, m)$.

**Output**

$B$ updated according to $B = \text{alpha} \times \text{op}(A) \times B$ or $B = \text{alpha} \times B \times \text{op}(A)$.
Reference: http://www.netlib.org/blas/strmm.f
Error status for this function can be retrieved via cublasGetError().

Error Status

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<td>CUBLAS_STATUS_EXECUTION_FAILED</td>
<td>if function failed to launch on GPU</td>
</tr>
</tbody>
</table>

Function cublasStrsm()

```c
void

void cublasStrsm (char side, char uplo, char transa,
     char diag, int m, int n, float alpha,
     const float *A, int lda, float *B, int ldb)
```

solves one of the matrix equations

\[
\text{op}(A) * X = \alpha B \quad \text{or} \quad X * \text{op}(A) = \alpha B,
\]

where \( \text{op}(A) = A \) or \( \text{op}(A) = A^T \),

\( \alpha \) is a single-precision scalar, and \( X \) and \( B \) are \( m \times n \) matrices that consist of single-precision elements. \( A \) is a unit or non-unit, upper or lower, triangular matrix.

The result matrix \( X \) overwrites input matrix \( B \); that is, on exit the result is stored in \( B \). Matrices \( A \) and \( B \) are stored in column-major format, and \( lda \) and \( ldb \) are the leading dimensions of the two-dimensional arrays that contain \( A \) and \( B \), respectively.

Input

- `side`: specifies whether \( \text{op}(A) \) appears on the left or right of \( X \):
  - `side` == 'L' or 'l' indicates solve \( \text{op}(A) * X = \alpha B \);
  - `side` == 'R' or 'r' indicates solve \( X * \text{op}(A) = \alpha B \).

- `uplo`: specifies whether the matrix \( A \) is an upper or lower triangular matrix:
  - `uplo` == 'U' or 'u' indicates \( A \) is an upper triangular matrix;
  - `uplo` == 'L' or 'l' indicates \( A \) is a lower triangular matrix.

- `transa`: specifies the form of \( \text{op}(A) \) to be used in matrix multiplication.
  - If `transa` == 'N' or 'n', \( \text{op}(A) = A \).
  - If `transa` == 'T', 't', 'C', or 'c', \( \text{op}(A) = A^T \).

- `diag`: specifies whether or not \( A \) is a unit triangular matrix.
  - If `diag` == 'U' or 'u', \( A \) is assumed to be unit triangular.
  - If `diag` == 'N' or 'n', \( A \) is not assumed to be unit triangular.
Input (continued)

- **m**: specifies the number of rows of B; m must be at least zero.
- **n**: specifies the number of columns of B; n must be at least zero.
- **alpha**: single-precision scalar multiplier applied to B. When alpha is zero, A is not referenced and B does not have to be a valid input.
- **A**: single-precision array of dimensions (lda, k), where k = m when side == 'L' or 'l', and is n when side == 'R' or 'r'. If uplo == 'U' or 'u', the leading k×k upper triangular part of the array A must contain the upper triangular matrix, and the strictly lower triangular matrix of A is not referenced. When uplo == 'L' or 'l', the leading k×k lower triangular part of the array A must contain the lower triangular matrix, and the strictly upper triangular part of A is not referenced. Note that when diag == 'U' or 'u', the diagonal elements of A are not referenced and are assumed to be unity.
- **lda**: leading dimension of the two-dimensional array containing A. When side == 'L' or 'l', lda must be at least max(1, m). When side == 'R' or 'r', lda must be at least max(1, n).
- **B**: single-precision array of dimensions (ldb, n); ldb must be at least max(1, m). The leading m×n part of the array B must contain the right-hand side matrix B. On exit B is overwritten by the solution matrix X.
- **ldb**: leading dimension of the two-dimensional array containing B; ldb must be at least max(1, m).

Output

- **B**: contains the solution matrix X satisfying op(A) * X = alpha * B or X * op(A) = alpha * B.

Reference: [http://www.netlib.org/blas/strsm.f](http://www.netlib.org/blas/strsm.f)

Error status for this function can be retrieved via `cublasGetError()`. Error Status:

- **CUBLAS_STATUS_NOT_INITIALIZED**: if CUBLAS library was not initialized
- **CUBLAS_STATUS_INVALID_VALUE**: if m < 0 or n < 0
- **CUBLAS_STATUS_EXECUTION_FAILED**: if function failed to launch on GPU
Single-Precision Complex BLAS3 Functions

The only single-precision complex BLAS3 function is `cublasCgemm()`.

Function `cublasCgemm()`

```c
void

`cublasCgemm (char transa, char transb, int m, int n, int k, cuComplex alpha, const cuComplex *A, int lda, const cuComplex *B, int ldb, cuComplex beta, cuComplex *C, int ldc)`

performs one of the matrix-matrix operations

\[ C = \alpha \circ \text{op}(A) \circ \text{op}(B) + \beta \circ C, \]

where \( \text{op}(X) = X, \text{op}(X) = X^T, \text{or} \: \text{op}(X) = X^H; \)

and \( \alpha \) and \( \beta \) are single-precision complex scalars. \( A, B, \) and \( C \) are matrices consisting of single-precision complex elements, with \( \text{op}(A) \) an \( m \times k \) matrix, \( \text{op}(B) \) a \( k \times n \) matrix and \( C \) an \( m \times n \) matrix.

Input

- **transa** specifies \( \text{op}(A) \). If \( \text{transa} == 'N' \) or \( 'n' \), \( \text{op}(A) = A \).
  - If \( \text{transa} == 'T' \) or \( 't' \), \( \text{op}(A) = A^T \).
  - If \( \text{transa} == 'C' \) or \( 'c' \), \( \text{op}(A) = A^H \).
- **transb** specifies \( \text{op}(B) \). If \( \text{transb} == 'N' \) or \( 'n' \), \( \text{op}(B) = B \).
  - If \( \text{transb} == 'T' \) or \( 't' \), \( \text{op}(B) = B^T \).
  - If \( \text{transb} == 'C' \) or \( 'c' \), \( \text{op}(B) = B^H \).
- **m** number of rows of matrix \( \text{op}(A) \) and rows of matrix \( C \);
  - \( m \) must be at least zero.
- **n** number of columns of matrix \( \text{op}(B) \) and number of columns of \( C \);
  - \( n \) must be at least zero.
- **k** number of columns of matrix \( \text{op}(A) \) and number of rows of \( \text{op}(B) \);
  - \( k \) must be at least zero.
- **alpha** single-precision complex scalar multiplier applied to \( \text{op}(A) \ast \text{op}(B) \).
- **A** single-precision complex array of dimension \((\text{lda}, k)\) if \( \text{transa} == 'N' \) or \( 'n' \), and of dimension \((\text{lda}, m)\) otherwise.
- **lda** leading dimension of \( A \). When \( \text{transa} == 'N' \) or \( 'n' \), it must be at least \( \max(1, m) \) and at least \( \max(1, k) \) otherwise.
B  single-precision complex array of dimension (ldb, n) if transB == 'N' or 'n', and of dimension (ldb, k) otherwise.

ldb  leading dimension of B. When transB == 'N' or 'n', it must be at least max(1, k) and at least max(1, n) otherwise.

beta  single-precision complex scalar multiplier applied to C. If beta is zero, C does not have to be a valid input.

C  single-precision array of dimensions (ldc, n).

ldc  leading dimension of C; ldc must be at least max(1, m).

Output
C  updated according to C = alpha * op(A) * op(B) + beta * C.

Reference: http://www.netlib.org/blas/cgemm.f

Error status for this function can be retrieved via cublasGetError().

Error Status

- **CUBLAS_STATUS_NOT_INITIALIZED**  if CUBLAS library was not initialized
- **CUBLAS_STATUS_INVALID_VALUE**  if m < 0, n < 0, or k < 0
- **CUBLAS_STATUS_EXECUTION_FAILED**  if function failed to launch on GPU
Double-Precision BLAS3 Functions

Note: Double-precision functions are only supported on GPUs with double-precision hardware.

The double-precision BLAS3 functions are listed below:

- “Function cublasDgemm()” on page 97
- “Function cublasDsymm()” on page 99
- “Function cublasDsyrk()” on page 101
- “Function cublasDsysr2k()” on page 103
- “Function cublasDtrmm()” on page 105
- “Function cublasDtrsm()” on page 107

Function cublasDgemm()

```c
void
cublasDgemm (char transa, char transb, int m, int n,
int k, double alpha, const double *A,
int lda, const double *B, int ldb,
double beta, double *C, int ldc)
```

computes the product of matrix A and matrix B, multiplies the result by scalar alpha, and adds the sum to the product of matrix C and scalar beta. It performs one of the matrix-matrix operations:

\[ C = \alpha \cdot \text{op}(A) \cdot \text{op}(B) + \beta \cdot C, \]

where \( \text{op}(X) = X \) or \( \text{op}(X) = X^T \),

and alpha and beta are double-precision scalars. A, B, and C are matrices consisting of double-precision elements, with \( \text{op}(A) \) an \( m \times k \) matrix, \( \text{op}(B) \) a \( k \times n \) matrix, and C an \( m \times n \) matrix. Matrices A, B, and C are stored in column-major format, and lda, ldb, and ldc are the
leading dimensions of the two-dimensional arrays containing A, B, and C.

**Input**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>transa</code></td>
<td>specifies ( \text{op}(A) ). If <code>transa == 'N'</code> or <code>'n'</code>, ( \text{op}(A) = A ). If <code>transa == 'T'</code>, <code>'t'</code>, <code>'C'</code>, or <code>'c'</code>, ( \text{op}(A) = A^T ).</td>
</tr>
<tr>
<td><code>transb</code></td>
<td>specifies ( \text{op}(B) ). If <code>transb == 'N'</code> or <code>'n'</code>, ( \text{op}(B) = B ). If <code>transb == 'T'</code>, <code>'t'</code>, <code>'C'</code>, or <code>'c'</code>, ( \text{op}(B) = B^T ).</td>
</tr>
<tr>
<td><code>m</code></td>
<td>number of rows of matrix ( \text{op}(A) ) and rows of matrix C; ( m ) must be at least zero.</td>
</tr>
<tr>
<td><code>n</code></td>
<td>number of columns of matrix ( \text{op}(B) ) and number of columns of C; ( n ) must be at least zero.</td>
</tr>
<tr>
<td><code>k</code></td>
<td>number of columns of matrix ( \text{op}(A) ) and number of rows of ( \text{op}(B) ); ( k ) must be at least zero.</td>
</tr>
<tr>
<td><code>alpha</code></td>
<td>double-precision scalar multiplier applied to ( \text{op}(A) ) * ( \text{op}(B) ).</td>
</tr>
<tr>
<td><code>A</code></td>
<td>double-precision array of dimensions ( (\text{lda}, k) ) if <code>transa == 'N'</code> or <code>'n'</code>, and of dimensions ( (\text{lda}, m) ) otherwise. If <code>transa == 'N'</code> or <code>'n'</code>, ( \text{lda} ) must be at least ( \max(1, m) ); otherwise, ( \text{lda} ) must be at least ( \max(1, k) ).</td>
</tr>
<tr>
<td><code>lda</code></td>
<td>leading dimension of two-dimensional array used to store matrix A.</td>
</tr>
<tr>
<td><code>B</code></td>
<td>double-precision array of dimensions ( (\text{ldb}, n) ) if <code>transb == 'N'</code> or <code>'n'</code>, and of dimensions ( (\text{ldb}, k) ) otherwise. If <code>transb == 'N'</code> or <code>'n'</code>, ( \text{ldb} ) must be at least ( \max(1, k) ); otherwise, ( \text{ldb} ) must be at least ( \max(1, n) ).</td>
</tr>
<tr>
<td><code>ldb</code></td>
<td>leading dimension of two-dimensional array used to store matrix B.</td>
</tr>
<tr>
<td><code>beta</code></td>
<td>double-precision scalar multiplier applied to ( C ). If zero, ( C ) does not have to be a valid input.</td>
</tr>
<tr>
<td><code>C</code></td>
<td>double-precision array of dimensions ( (\text{ldc}, n) ); ( \text{ldc} ) must be at least ( \max(1, m) ).</td>
</tr>
<tr>
<td><code>ldc</code></td>
<td>leading dimension of two-dimensional array used to store matrix C.</td>
</tr>
</tbody>
</table>

**Output**

\[ C \] updated based on \( C = \alpha \cdot \text{op}(A) \cdot \text{op}(B) + \beta \cdot C \).

**Reference:** [http://www.netlib.org/blas/dgemm.f](http://www.netlib.org/blas/dgemm.f)

Error status for this function can be retrieved via `cublasGetError()`.  

**Error Status**

- `CUBLAS_STATUS_NOT_INITIALIZED` if CUBLAS library was not initialized  
- `CUBLAS_STATUS_INVALID_VALUE` if \( m < 0 \), \( n < 0 \), or \( k < 0 \)
Error Status (continued)

<table>
<thead>
<tr>
<th>Status Code</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CUBLAS_STATUS_ARCH_MISMATCH</td>
<td>if function invoked on device that does not support double precision</td>
</tr>
<tr>
<td>CUBLAS_STATUS_EXECUTION_FAILED</td>
<td>if function failed to launch on GPU</td>
</tr>
</tbody>
</table>

Function cublasDsymm()

```c
void

```
cublasDsymm (char side, char uplo, int m, int n,
               double alpha, const double *A, int lda,
               const double *B, int ldb, double beta,
               double *C, int ldc)
```

performs one of the matrix-matrix operations

\[
C = \alpha A \ast B + \beta C \quad \text{or} \quad C = \alpha B \ast A + \beta C,
\]

where \(\alpha\) and \(\beta\) are double-precision scalars, \(A\) is a symmetric matrix consisting of double-precision elements and is stored in either lower or upper storage mode. \(B\) and \(C\) are \(m \times n\) matrices consisting of double-precision elements.

**Input**

- **side**: specifies whether the symmetric matrix \(A\) appears on the left-hand side or right-hand side of matrix \(B\).
  - If `side` \(\equiv \) 'L' or 'l', \(C = \alpha A \ast B + \beta C\).
  - If `side` \(\equiv \) 'R' or 'r', \(C = \alpha B \ast A + \beta C\).

- **uplo**: specifies whether the symmetric matrix \(A\) is stored in upper or lower storage mode. If `uplo` \(\equiv \) 'U' or 'u', only the upper triangular part of the symmetric matrix is referenced, and the elements of the strictly lower triangular part are inferred from those in the upper triangular part. If `uplo` \(\equiv \) 'L' or 'l', only the lower triangular part of the symmetric matrix is referenced, and the elements of the strictly upper triangular part are inferred from those in the lower triangular part.

- **m**: specifies the number of rows of matrix \(C\), and the number of rows of matrix \(B\). It also specifies the dimensions of symmetric matrix \(A\) when `side` \(\equiv \) 'L' or 'l'; \(m\) must be at least zero.

- **n**: specifies the number of columns of matrix \(C\), and the number of columns of matrix \(B\). It also specifies the dimensions of symmetric matrix \(A\) when `side` \(\equiv \) 'R' or 'r'; \(n\) must be at least zero.

- **alpha**: double-precision scalar multiplier applied to \(A \ast B\) or \(B \ast A\).
Input (continued)

- **A**: double-precision array of dimensions $(\text{lda}, \text{ka})$, where $\text{ka}$ is $m$ when $\text{side} == 'L' \text{ or } 'l'$, and $n$ otherwise. If $\text{side} == 'L' \text{ or } 'l'$, the leading $m \times m$ part of array $A$ must contain the symmetric matrix, such that when $\text{uplo} == 'U' \text{ or } 'u'$, the leading $m \times m$ part stores the upper triangular part of the symmetric matrix, and the strictly lower triangular part of $A$ is not referenced; and when $\text{uplo} == 'L' \text{ or } 'l'$, the leading $m \times m$ part stores the lower triangular part of the symmetric matrix and the strictly upper triangular part is not referenced. If $\text{side} == 'R' \text{ or } 'r'$, the leading $n \times n$ part of array $A$ must contain the symmetric matrix, such that when $\text{uplo} == 'U' \text{ or } 'u'$, the leading $n \times n$ part stores the upper triangular part of the symmetric matrix and the strictly lower triangular part of $A$ is not referenced; and when $\text{uplo} == 'L' \text{ or } 'l'$, the leading $n \times n$ part stores the lower triangular part of the symmetric matrix and the strictly upper triangular part is not referenced.

- **lda**: leading dimension of $A$. When $\text{side} == 'L' \text{ or } 'l'$, it must be at least $\max(1, m)$ and at least $\max(1, n)$ otherwise.

- **B**: double-precision array of dimensions $(\text{ldb}, n)$. On entry, the leading $m \times n$ part of the array contains the matrix $B$.

- **ldb**: leading dimension of $B$; $\text{ldb}$ must be at least $\max(1, m)$.

- **beta**: double-precision scalar multiplier applied to $C$. If $\text{beta}$ is zero, $C$ does not have to be a valid input.

- **C**: double-precision array of dimensions $(\text{ldc}, n)$.

- **ldc**: leading dimension of $C$; $\text{ldc}$ must be at least $\max(1, m)$.

Output

Updated according to $C = \alpha \cdot A \cdot B + \beta \cdot C$ or $C = \alpha \cdot B \cdot A + \beta \cdot C$.

Reference: [http://www.netlib.org/blas/dsymm.f](http://www.netlib.org/blas/dsymm.f)

Error status for this function can be retrieved via `cublasGetError()`.

Error Status

- **CUBLAS_STATUS_NOT_INITIALIZED**: if CUBLAS library was not initialized

- **CUBLAS_STATUS_INVALID_VALUE**: if $m < 0$, $n < 0$, or $k < 0$

- **CUBLAS_STATUS_ARCH_MISMATCH**: if function invoked on device that does not support double precision

- **CUBLAS_STATUS_EXECUTION_FAILED**: if function failed to launch on GPU
Function cublasDsyrk()

```c
void
cublasDsyrk (char uplo, char trans, int n, int k,
double alpha, const double *A, int lda,
double beta, double *C, int ldc)
```

performs one of the symmetric rank $k$ operations

$$C = \alpha A A^T + \beta C \text{ or } C = \alpha A^T A + \beta C,$$

where $\alpha$ and $\beta$ are double-precision scalars. $C$ is an $n \times n$ symmetric matrix consisting of double-precision elements and is stored in either lower or upper storage mode. $A$ is a matrix consisting of double-precision elements with dimensions of $n \times k$ in the first case, and $k \times n$ in the second case.

**Input**

- **uplo** specifies whether the symmetric matrix $C$ is stored in upper or lower storage mode. If $\text{uplo} == 'U'$ or 'u', only the upper triangular part of the symmetric matrix is referenced, and the elements of the strictly lower triangular part are inferred from those in the upper triangular part. If $\text{uplo} == 'L'$ or 'l', only the lower triangular part of the symmetric matrix is referenced, and the elements of the strictly upper triangular part are inferred from those in the lower triangular part.

- **trans** specifies the operation to be performed. If $\text{trans} == 'N'$ or 'n', $C = \alpha A A^T + \beta C$. If $\text{trans} == 'T'$, 't', 'C', or 'c', $C = \alpha A^T A + \beta C$.

- **n** specifies the number of rows and the number columns of matrix $C$. If $\text{trans} == 'N'$ or 'n', $n$ specifies the number of rows of matrix $A$. If $\text{trans} == 'T'$, 't', 'C', or 'c', $n$ specifies the number of columns of matrix $A$; $n$ must be at least zero.

- **k** If $\text{trans} == 'N'$ or 'n', $k$ specifies the number of columns of matrix $A$. If $\text{trans} == 'T'$, 't', 'C', or 'c', $k$ specifies the number of rows of matrix $A$; $k$ must be at least zero.

- **alpha** double-precision scalar multiplier applied to $A A^T$ or $A^T A$.

- **A** double-precision array of dimensions (lda, ka), where ka is $k$ when $\text{trans} == 'N'$ or 'n', and is $n$ otherwise. When $\text{trans} == 'N'$ or 'n', the leading $n \times k$ part of array $A$ contains the matrix $A$; otherwise, the leading $k \times n$ part of the array contains the matrix $A$.

- **lda** leading dimension of $A$. When $\text{trans} == 'N'$ or 'n', lda must be at least $\max(1, n)$. Otherwise lda must be at least $\max(1, k)$. 


Input (continued)

- **beta**
  - double-precision scalar multiplier applied to C.
  - If beta is zero, C is not read.

- **C**
  - double-precision array of dimensions (ldc, n). If uplo == 'U' or 'u', the leading n×n triangular part of the array C must contain the upper triangular part of the symmetric matrix C, and the strictly lower triangular part of C is not referenced. On exit, the upper triangular part of C is overwritten by the upper triangular part of the updated matrix. If uplo == 'L' or 'l', the leading n×n triangular part of the array C must contain the lower triangular part of the symmetric matrix C, and the strictly upper triangular part of C is not referenced. On exit, the lower triangular part of C is overwritten by the lower triangular part of the updated matrix.

- **ldc**
  - leading dimension of C; ldc must be at least max(1, n).

Output

- C updated according to C = alpha * A * A^T + beta * C or C = alpha * A^T * A + beta * C.

Reference: [http://www.netlib.org/blas/dsyrk.f](http://www.netlib.org/blas/dsyrk.f)

Error status for this function can be retrieved via cublasGetError().

Error Status

- **CUBLAS_STATUS_NOT_INITIALIZED** if CUBLAS library was not initialized
- **CUBLAS_STATUS_INVALID_VALUE** if m < 0, n < 0, or k < 0
- **CUBLAS_STATUS_ARCH_MISMATCH** if function invoked on device that does not support double precision
- **CUBLAS_STATUS_EXECUTION_FAILED** if function failed to launch on GPU
**Function cublasDsyr2k()**

```c
void cublasDsyr2k (char uplo, char trans, int n, int k, 
    double alpha, const double *A, int lda, 
    const double *B, int ldb, double beta, 
    double *C, int ldc)
```

performs one of the symmetric rank 2k operations

\[
C = \alpha A \cdot B^T + \alpha B \cdot A^T + \beta C \quad \text{or} \\
C = \alpha A^T \cdot B + \alpha B^T \cdot A + \beta C,
\]

where \(\alpha\) and \(\beta\) are double-precision scalars. \(C\) is an \(n \times n\) symmetric matrix consisting of double-precision elements and is stored in either lower or upper storage mode. \(A\) and \(B\) are matrices consisting of double-precision elements with dimension of \(n \times k\) in the first case, and \(k \times n\) in the second case.

**Input**

- `uplo` specifies whether the symmetric matrix \(C\) is stored in upper or lower storage mode. If `uplo` == `'U'` or `'u'`, only the upper triangular part of the symmetric matrix is referenced, and the elements of the strictly lower triangular part are inferred from those in the upper triangular part. If `uplo` == `'L'` or `'l'`, only the lower triangular part of the symmetric matrix is referenced, and the elements of the strictly upper triangular part are inferred from those in the lower triangular part.

- `trans` specifies the operation to be performed. If `trans` == `'N'` or `'n'`, \(C = \alpha A \cdot B^T + \alpha B \cdot A^T + \beta C\). If `trans` == `'T'`, `'t'`, `'C'`, or `'c'`, \(C = \alpha A^T \cdot B + \alpha B^T \cdot A + \beta C\).

- `n` specifies the number of rows and the number columns of matrix \(C\). If `trans` == `'N'` or `'n'`, \(n\) specifies the number of rows of matrix \(A\). If `trans` == `'T'`, `'t'`, `'C'`, or `'c'`, \(n\) specifies the number of columns of matrix \(A\); \(n\) must be at least zero.

- `k` specifies the number of columns of matrix \(A\). If `trans` == `'N'` or `'n'`, \(k\) specifies the number of columns of matrix \(A\). If `trans` == `'T'`, `'t'`, `'C'`, or `'c'`, \(k\) specifies the number of rows of matrix \(A\); \(k\) must be at least zero.

- `alpha` double-precision scalar multiplier.

- `A` double-precision array of dimensions \((lda, ka)\), where \(ka\) is \(k\) when `trans` == `'N'` or `'n'`, and is \(n\) otherwise. When `trans` == `'N'` or `'n'`, the leading \(n \times k\) part of array \(A\) must contain the matrix \(A\), otherwise the leading \(k \times n\) part of the array must contain the matrix \(A\).
Input (continued)

lda  leading dimension of A. When trans == 'N' or 'n', lda must be at least max(1, n). Otherwise lda must be at least max(1, k).

B  double-precision array of dimensions (lda, kb), where kb = k when trans == 'N' or 'n', and k = n otherwise. When trans == 'N' or 'n', the leading n×k part of array B must contain the matrix B, otherwise the leading k×n part of the array must contain the matrix B.

ldb  leading dimension of B. When trans == 'N' or 'n', ldb must be at least max(1, n). Otherwise ldb must be at least max(1, k).

beta  double-precision scalar multiplier applied to C. If beta is zero, C does not have to be a valid input.

C  double-precision array of dimensions (ldc, n). If uplo == 'U' or 'u', the leading n×n triangular part of the array C must contain the upper triangular part of the symmetric matrix C, and the strictly lower triangular part of C is not referenced. On exit, the upper triangular part of C is overwritten by the upper triangular part of the updated matrix. If uplo == 'L' or 'l', the leading n×n triangular part of the array C must contain the lower triangular part of the symmetric matrix C, and the strictly upper triangular part of C is not referenced. On exit, the lower triangular part of C is overwritten by the lower triangular part of the updated matrix.

ldc  leading dimension of C; ldc must be at least max(1, n).

Output

C  updated according to

\[
C = \alpha \cdot A \cdot B^T + \alpha \cdot B \cdot A^T + \beta \cdot C \quad \text{or} \\
C = \alpha \cdot A^T \cdot B + \alpha \cdot B^T \cdot A + \beta \cdot C.
\]

Reference: http://www.netlib.org/blas/dsyrk.f

Error status for this function can be retrieved via cublasGetError().

Error Status

<table>
<thead>
<tr>
<th>Status</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CUBLAS_STATUS_NOT_INITIALIZED</td>
<td>if CUBLAS library was not initialized</td>
</tr>
<tr>
<td>CUBLAS_STATUS_INVALID_VALUE</td>
<td>if m &lt; 0, n &lt; 0, or k &lt; 0</td>
</tr>
<tr>
<td>CUBLAS_STATUS_ARCH_MISMATCH</td>
<td>if function invoked on device that does not support double precision</td>
</tr>
<tr>
<td>CUBLAS_STATUS_EXECUTION_FAILED</td>
<td>if function failed to launch on GPU</td>
</tr>
</tbody>
</table>
Function cublasDtrmm()

```c
void
cublasDtrmm (char side, char uplo, char transa,
        char diag, int m, int n, double alpha,
        const double *A, int lda, const double *B,
        int ldb)
```

performs one of the matrix-matrix operations

\[
B = \alpha \operatorname{op}(A) \times B \quad \text{or} \quad B = \alpha \times \operatorname{B} \times \operatorname{op}(A),
\]

where \( \operatorname{op}(A) = A \) \( \text{or} \) \( \operatorname{op}(A) = A^T \),

\( \alpha \) is a double-precision scalar, \( B \) is an \( m \times n \) matrix consisting of double-precision elements, and \( A \) is a unit or non-unit, upper or lower triangular matrix consisting of double-precision elements.

Matrices \( A \) and \( B \) are stored in column-major format, and \( \text{lda} \) and \( \text{ldb} \) are the leading dimensions of the two-dimensional arrays that contain \( A \) and \( B \), respectively.

**Input**

- **side** specifies whether \( \operatorname{op}(A) \) multiplies \( B \) from the left or right.
  - If \( \text{side} == 'L' \) or \( 'l' \), \( B = \alpha \times \operatorname{op}(A) \times B \).
  - If \( \text{side} == 'R' \) or \( 'r' \), \( B = \alpha \times \operatorname{B} \times \operatorname{op}(A) \).
- **uplo** specifies whether the matrix \( A \) is an upper or lower triangular matrix.
  - If \( \text{uplo} == 'U' \) or \( 'u' \), \( A \) is an upper triangular matrix.
  - If \( \text{uplo} == 'L' \) or \( 'l' \), \( A \) is a lower triangular matrix.
- **transa** specifies the form of \( \operatorname{op}(A) \) to be used in the matrix multiplication.
  - If \( \text{transa} == 'N' \) or \( 'n' \), \( \operatorname{op}(A) = A \).
  - If \( \text{transa} == 'T' \), \( 't' \), \( 'C' \), or \( 'c' \), \( \operatorname{op}(A) = A^T \).
- **diag** specifies whether or not \( A \) is a unit triangular matrix. If \( \text{diag} == 'U' \) or \( 'u' \), \( A \) is assumed to be unit triangular. If \( \text{diag} == 'N' \) or \( 'n' \), \( A \) is not assumed to be unit triangular.
- **m** the number of rows of matrix \( B \); \( m \) must be at least zero.
- **n** the number of columns of matrix \( B \); \( n \) must be at least zero.
- **alpha** double-precision scalar multiplier applied to \( \operatorname{op}(A) \times B \) \( \text{or} \) \( B \times \operatorname{op}(A) \), respectively. If \( \alpha \) is zero, no accesses are made to matrix \( A \), and no read accesses are made to matrix \( B \).
Input (continued)

A  double-precision array of dimensions (lda, k). If side == 'L' or 'l', k = m. If side == 'R' or 'r', k = n. If uplo == 'U' or 'u', the leading k×k upper triangular part of the array A must contain the upper triangular matrix, and the strictly lower triangular part of A is not referenced. If uplo == 'L' or 'l', the leading k×k lower triangular part of the array A must contain the lower triangular matrix, and the strictly upper triangular part of A is not referenced. When diag == 'U' or 'u', the diagonal elements of A are not referenced and are assumed to be unity.

lda  leading dimension of A. When side == 'L' or 'l', it must be at least max(1, m) and at least max(1, n) otherwise.

B  double-precision array of dimensions (ldb, n). On entry, the leading m×n part of the array contains the matrix B. It is overwritten with the transformed matrix on exit.

ldb  leading dimension of B; ldb must be at least max(1, m).

Output

B  updated according to B = alpha * op(A) * B or B = alpha * B * op(A).

Reference: http://www.netlib.org/blas/dtrmm.f

Error status for this function can be retrieved via cublasGetError().

Error Status

CUBLAS_STATUS_NOT_INITIALIZED  if CUBLAS library was not initialized
CUBLAS_STATUS_INVALID_VALUE  if m < 0, n < 0, or k < 0
CUBLAS_STATUS_ARCH_MISMATCH  if function invoked on device that does not support double precision
CUBLAS_STATUS_EXECUTION_FAILED  if function failed to launch on GPU
Function cublasDtrsm()

```c
void
cublasDtrsm (char side, char uplo, char transa,
            char diag, int m, int n, double alpha,
            const double *A, int lda, double *B,
            int ldb)
```

solves one of the matrix equations

\[
\text{op}(A) \cdot X = \alpha \cdot B \quad \text{or} \quad X \cdot \text{op}(A) = \alpha \cdot B,
\]

where \( \text{op}(A) = A \) or \( \text{op}(A) = A^T \).

\( \alpha \) is a double-precision scalar, and \( X \) and \( B \) are \( m \times n \) matrices that consist of double-precision elements. \( A \) is a unit or non-unit, upper or lower, triangular matrix.

The result matrix \( X \) overwrites input matrix \( B \); that is, on exit the result is stored in \( B \). Matrices \( A \) and \( B \) are stored in column-major format, and \( lda \) and \( ldb \) are the leading dimensions of the two-dimensional arrays that contain \( A \) and \( B \), respectively.

**Input**

- **side** specifies whether \( \text{op}(A) \) appears on the left or right of \( X \):
  - side == 'L' or 'l' indicates solve \( \text{op}(A) \cdot X = \alpha \cdot B \);
  - side == 'R' or 'r' indicates solve \( X \cdot \text{op}(A) = \alpha \cdot B \).

- **uplo** specifies whether the matrix \( A \) is an upper or lower triangular matrix:
  - uplo == 'U' or 'u' indicates \( A \) is an upper triangular matrix;
  - uplo == 'L' or 'l' indicates \( A \) is a lower triangular matrix.

- **transa** specifies the form of \( \text{op}(A) \) to be used in matrix multiplication.
  - If transa == 'N' or 'n', \( \text{op}(A) = A \).
  - If transa == 'T', 't', 'C', or 'c', \( \text{op}(A) = A^T \).

- **diag** specifies whether or not \( A \) is a unit triangular matrix.
  - If diag == 'U' or 'u', \( A \) is assumed to be unit triangular.
  - If diag == 'N' or 'n', \( A \) is not assumed to be unit triangular.

- **m** specifies the number of rows of \( B \); \( m \) must be at least zero.

- **n** specifies the number of columns of \( B \); \( n \) must be at least zero.

- **alpha** double-precision scalar multiplier applied to \( B \). When \( \alpha \) is zero, \( A \) is not referenced and \( B \) does not have to be a valid input.
CUDA

CUDA CUBLAS Library

Reference: http://www.netlib.org/blas/dtrsm.f

Error status for this function can be retrieved via cublasGetError().

Error Status

- **CUBLAS_STATUS_NOT_INITIALIZED** if CUBLAS library was not initialized
- **CUBLAS_STATUS_INVALID_VALUE** if \( m < 0, n < 0, \) or \( k < 0 \)
- **CUBLAS_STATUS_ARCH_MISMATCH** if function invoked on device that does not support double precision
- **CUBLAS_STATUS_EXECUTION_FAILED** if function failed to launch on GPU

Input (continued)

- **A** - double-precision array of dimensions \((\text{lda}, k)\), where \( k = m \) when \( \text{side} == 'L' \) or \( 'l' \), and is \( n \) when \( \text{side} == 'R' \) or \( 'r' \). If \( \text{uplo} == 'U' \) or \( 'u' \), the leading \( k \times k \) upper triangular part of the array \( A \) must contain the upper triangular matrix, and the strictly lower triangular matrix of \( A \) is not referenced. When \( \text{uplo} == 'L' \) or \( 'l' \), the leading \( k \times k \) lower triangular part of the array \( A \) must contain the lower triangular matrix, and the strictly upper triangular part of \( A \) is not referenced. Note that when \( \text{diag} == 'U' \) or \( 'u' \), the diagonal elements of \( A \) are not referenced and are assumed to be unity.

- **lda** - leading dimension of the two-dimensional array containing \( A \). When \( \text{side} == 'L' \) or \( 'l' \), \( \text{lda} \) must be at least \( \text{max}(1, m) \). When \( \text{side} == 'R' \) or \( 'r' \), \( \text{lda} \) must be at least \( \text{max}(1, n) \).

- **B** - double-precision array of dimensions \((\text{ldb}, n)\); \( \text{ldb} \) must be at least \( \text{max}(1, m) \). The leading \( m \times n \) part of the array \( B \) must contain the right-hand side matrix \( B \). On exit, \( B \) is overwritten by the solution matrix \( X \).

- **ldb** - leading dimension of the two-dimensional array containing \( B \); \( \text{ldb} \) must be at least \( \text{max}(1, m) \).

Output

- **B** contains the solution matrix \( X \) satisfying \( \text{op}(A) \times X = \alpha \times B \) or \( X \times \text{op}(A) = \alpha \times B \).
Double-Precision Complex BLAS3 Functions

Note: Double-precision functions are only supported on GPUs with double-precision hardware.

The only currently implemented double-precision complex BLAS3 function is `cublasZgemm()`.

Function `cublasZgemm()`

```c
void

cublasZgemm (char transa, char transb, int m, int n,
int k, cuDoubleComplex alpha,
const cuDoubleComplex *A, int lda,
const cuDoubleComplex *B, int ldb,
cuDoubleComplex beta, cuDoubleComplex *C,
int ldc)
```
performs one of the matrix-matrix operations

\[
C = \alpha \cdot \text{op}(A) \cdot \text{op}(B) + \beta \cdot C,
\]

where \( \text{op}(X) = X, \text{op}(X) = X^T, \) or \( \text{op}(X) = X^H; \)

and \( \alpha \) and \( \beta \) are double-precision complex scalars. \( A, B, \) and \( C \) are matrices consisting of double-precision complex elements, with \( \text{op}(A) \) an \( m \times k \) matrix, \( \text{op}(B) \) a \( k \times n \) matrix and \( C \) an \( m \times n \) matrix.

Input

- `transa` specifies \( \text{op}(A) \). If `transa` == ’N’ or ’n’, \( \text{op}(A) \) = \( A \).
  - If `transa` == ’T’ or ’t’, \( \text{op}(A) \) = \( A^T \).
  - If `transa` == ’C’ or ’c’, \( \text{op}(A) \) = \( A^H \).
- `transb` specifies \( \text{op}(B) \). If `transb` == ’N’ or ’n’, \( \text{op}(B) \) = \( B \).
  - If `transb` == ’T’ or ’t’, \( \text{op}(B) \) = \( B^T \).
  - If `transb` == ’C’ or ’c’, \( \text{op}(B) \) = \( B^H \).
- `m` number of rows of matrix \( \text{op}(A) \) and rows of matrix \( C \); \( m \) must be at least zero.
- `n` number of columns of matrix \( \text{op}(B) \) and number of columns of \( C \); \( n \) must be at least zero.
- `k` number of columns of matrix \( \text{op}(A) \) and number of rows of \( \text{op}(B) \); \( k \) must be at least zero.
CUDA

Input (continued)

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>alpha</td>
<td>double-precision complex scalar multiplier applied to ( \alpha ) ( \text{op}(A) \times \text{op}(B) ).</td>
</tr>
<tr>
<td>A</td>
<td>double-precision complex array of dimension ((\text{lda}, k)) if (\text{transa} == \text{'N'}) or (\text{'n'}), and of dimension ((\text{lda}, m)) otherwise.</td>
</tr>
<tr>
<td>lda</td>
<td>leading dimension of (A). When (\text{transa} == \text{'N'}) or (\text{'n'}), it must be at least (\text{max}(1, m)) and at least (\text{max}(1, k)) otherwise.</td>
</tr>
<tr>
<td>B</td>
<td>double-precision complex array of dimension ((\text{ldb}, n)) if (\text{transb} == \text{'N'}) or (\text{'n'}), and of dimension ((\text{ldb}, k)) otherwise.</td>
</tr>
<tr>
<td>ldb</td>
<td>leading dimension of (B). When (\text{transb} == \text{'N'}) or (\text{'n'}), it must be at least (\text{max}(1, k)) and at least (\text{max}(1, n)) otherwise.</td>
</tr>
<tr>
<td>beta</td>
<td>double-precision complex scalar multiplier applied to (C). If (\beta) is zero, (C) does not have to be a valid input.</td>
</tr>
<tr>
<td>C</td>
<td>double-precision array of dimensions ((\text{ldc}, n)).</td>
</tr>
<tr>
<td>ldc</td>
<td>leading dimension of (C); (\text{ldc}) must be at least (\text{max}(1, m)).</td>
</tr>
</tbody>
</table>

Output

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>C</td>
<td>updated according to (C = \alpha \text{op}(A) \times \text{op}(B) + \beta C).</td>
</tr>
</tbody>
</table>

Reference: [http://www.netlib.org/blas/zgemm.f](http://www.netlib.org/blas/zgemm.f)

Error status for this function can be retrieved via \texttt{cublasGetError()}. Error Status

<table>
<thead>
<tr>
<th>Status Code</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>CUBLAS_STATUS_NOT_INITIALIZED</td>
<td>if CUBLAS library was not initialized</td>
</tr>
<tr>
<td>CUBLAS_STATUS_INVALID_VALUE</td>
<td>if (m &lt; 0), (n &lt; 0), or (k &lt; 0)</td>
</tr>
<tr>
<td>CUBLAS_STATUS_ARCH_MISMATCH</td>
<td>if function invoked on device that does not support double precision</td>
</tr>
<tr>
<td>CUBLAS_STATUS_EXECUTION_FAILED</td>
<td>if function failed to launch on GPU</td>
</tr>
</tbody>
</table>
CUBLAS Fortran Bindings

CUBLA is implemented using the C-based CUDA toolchain and thus provides a C-style API. This makes interfacing to applications written in C or C++ trivial. In addition, there are many applications implemented in Fortran that would benefit from using CUBLAS. CUBLAS uses 1-based indexing and Fortran-style column-major storage for multidimensional data to simplify interfacing to Fortran applications. Unfortunately, Fortran-to-C calling conventions are not standardized and differ by platform and toolchain. In particular, differences may exist in the following areas:

- Symbol names (capitalization, name decoration)
- Argument passing (by value or reference)
- Passing of string arguments (length information)
- Passing of pointer arguments (size of the pointer)
- Returning floating-point or compound data types (for example, single-precision or complex data types)

To provide maximum flexibility in addressing those differences, the CUBLAS Fortran interface is provided in the form of wrapper functions. These wrapper functions, written in C, are located in the file `fortran.c`, whose code needs to be compiled into an application for it to call the CUBLAS API functions. Providing source code allows users to make any changes necessary for a particular platform and toolchain.
The code in fortran.c has been used to demonstrate interoperability with the compilers g77 3.2.3 on 32-bit Linux, g77 3.4.5 on 64-bit Linux, Intel Fortran 9.0 and Intel Fortran 10.0 on 32-bit and 64-bit Microsoft Windows XP, and g77 3.4.0 on Mac OS X.

Note that for g77, use of the compiler flag -fno-second-underscore is required to use these wrappers as provided. Also, the use of the default calling conventions with regard to argument and return value passing is expected. Using the flag -fno-f2c changes the default calling convention with respect to these two items.

Two kinds of wrapper functions are provided. The thunking wrappers allow interfacing to existing Fortran applications without any changes to the applications. During each call, the wrappers allocate GPU memory, copy source data from CPU memory space to GPU memory space, call CUBLAS, and finally copy back the results to CPU memory space and deallocate the GPU memory. As this process causes very significant call overhead, these wrappers are intended for light testing, not for production code. By default, non-thunking wrappers are used for production code. To enable the thunking wrappers, symbol CUBLAS_USE_THUNKING must be defined for the compilation of fortran.c.

The non-thunking wrappers, intended for production code, substitute device pointers for vector and matrix arguments in all BLAS functions. To use these interfaces, existing applications need to be modified slightly to allocate and deallocate data structures in GPU memory space (using CUBLAS_ALLOC and CUBLAS_FREE) and to copy data between GPU and CPU memory spaces (using CUBLAS_SET_VECTOR, CUBLAS_GET_VECTOR, CUBLAS_SET_MATRIX, and CUBLAS_GET_MATRIX). The sample wrappers provided in fortran.c map device pointers to 32-bit integers on the Fortran side, regardless of whether the host platform is a 32-bit or 64-bit platform.

One approach to deal with index arithmetic on device pointers in Fortran code is to use C-style macros, and use the C preprocessor to expand these, as shown in the example below. On Linux and Mac OS X, one way of pre-processing is to invoke 'g77 -E -xf77-cpp-input'. On Windows platforms with Microsoft Visual C/C++, using 'cl -EP' achieves similar results.
When traditional fixed-form Fortran 77 code is ported to CUBLAS, line length often increases when the BLAS calls are exchanged for CUBLAS calls. Longer function names and possible macro expansion are contributing factors. Inadvertently exceeding the maximum line length can lead to run-time errors that are difficult to find, so care should be taken not to exceed the 72-column limit if fixed form is retained.

The following examples show a small application implemented in Fortran 77 on the host (Example A.1., “Fortran 77 Application Executing on the Host” on page 114), and show the same application using the non-thunking wrappers after it has been ported to use CUBLAS (Example A.2., “Fortran 77 Application Ported to Use CUBLAS” on page 115).
Example A.1. Fortran 77 Application Executing on the Host

```fortran
subroutine modify (m, ldm, n, p, q, alpha, beta)
imPLICIT none
INTEGER ldm, n, p, q
REAL*4 m(ldm,*), alpha, beta
EXTERNAL sscal
CALL sscal (n-p+1, alpha, m(p,q), ldm)
call sscal (ldm-p+1, beta, m(p,q), 1)
return
end

program matrixmod
implicit none
integer M, N
parameter (M=6, N=5)
real*4 a(M,N)
integer i, j
do j = 1, N
do i = 1, M
   a(i,j) = (i-1) * M + j
endo
doenddo
call modify (a, M, N, 2, 3, 16.0, 12.0)
do j = 1, N
do i = 1, M
   WRite(*,",(F7.0$") a(i,j)
endo
do
stop
end
```
Example A.2. Fortran 77 Application Ported to Use CUBLAS

```fortran
#define IDX2F(i,j,ld) (((j)-1)*(ld))+((i)-1))

subroutine modify (devPtrM, ldm, n, p, q, alpha, beta)
implicit none
integer sizeof_real
parameter (sizeof_real=4)
integer ldm, n, p, q, devPtrM
real*4 alpha, beta
call cublas_sscal (n-p+1, alpha,
1                   devPtrM+IDX2F(p,q,ldm)*sizeof_real,
2                   ldm)
call cublas_sscal (ldm-p+1, beta,
1                   devPtrM+IDX2F(p,q,ldm)*sizeof_real,
2                   1)
return
end

program matrixmod
implicit none
integer M, N, sizeof_real, devPtrA
parameter (M=6, N=5, sizeof_real=4)
real*4 a(M,N)
integer i, j, stat
external cublas_init, cublas_set_matrix, cublas_get_matrix
external cublas_shutdown, cublas_alloc
integer cublas_alloc, cublas_set_matrix, cublas_get_matrix
do j = 1, N
  do i = 1, M
    a(i,j) = (i-1) * M + j
  enddo
enddo

call cublas_init
stat = cublas_alloc(M*N, sizeof_real, devPtrA)
if (stat .NE. 0) then
```

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# CHAPTER A CUBLAS Fortran Bindings

NVIDIA

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PG-00000-002_V2.1 NVIDIA
Example A.2. Fortran 77 Application Ported to Use CUBLAS (continued)

```fortran
write(*,*) "device memory allocation failed"
call cublas_shutdown
stop
endif
stat = cublas_set_matrix (M, N, sizeof_real, a, M, devPtrA, M)
if (stat .NE. 0) then
call cublas_free (devPtrA)
write(*,*) "data download failed"
call cublas_shutdown
stop
endif
call modify (devPtrA, M, N, 2, 3, 16.0, 12.0)
stat = cublas_get_matrix (M, N, sizeof_real, devPtrA, M, a, M)
if (stat .NE. 0) then
call cublas_free (devPtrA)
write(*,*) "data upload failed"
call cublas_shutdown
stop
endif
call cublas_free (devPtrA)
call cublas_shutdown
do j = 1, N
  do i = 1, M
    write(*,"(F7.0$)") a(i,j)
  enddo
write (*,*) ""
enddo
stop
end
```